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A consistent set of nuclear rms charge radii: properties of the radius surface $R(N, Z)$ [☆]

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Abstract

A set of 799 ground state nuclear charge radii is presented. Experimental data from elastic electron scattering, muonic atom X-rays, K_{α} isotope shifts, and optical isotope shifts have been taken into account that were available up to January 2004. Wherever possible, connections and constraints between the data were applied to make the data system consistent. Based on the resulting data set, the smooth global structure of the radius surface $R(N, Z)$ was investigated by fitting simple empirical functions to the intersections with constant Z and N as well as with constant A plains. The simple behavior of the surface rendered it possible to apply a simple model, the two-liquid drop model to reproduce the main tendencies, and to predict the existence of a indentation along the line of stability on the radius surface. This indentation suggests a decrease of average nucleon density away from stability. The fine structure in the mass number dependence of rms charge radii is briefly presented.

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1. Introduction

The rms charge radius $\langle r^2 \rangle^{1/2}$ is a fundamental property of the atomic nucleus. It can be measured by two experimental methods: electron scattering (e^-) and muonic atom X-rays (μ^-), while the difference $\delta_{1,2} \langle r^2 \rangle \equiv \langle r^2 \rangle_{A2} - \langle r^2 \rangle_{A1}$ between two isotopes of the same element is determined by the K_z isotope shift ($K_z IS$) and by the isotope shift of optical spectrum lines (OIS). Early compilations [1–8] contained separate tables of results from the four different methods. It is of importance to derive radius values using the results of all experimental methods. This is also for the benefit of data users, who generally prefer a single, unified data set to several separate tables.

In 1994, a compilation of rms charge radii was published [9] comprising 523 ground state and 75 isomer radius data for isotopes of 42 elements. It was followed by another compilation [10], where the main emphasis was laid on the simultaneous evaluation of two experimental methods: $e^- + \mu^-$. Moreover, for nine elements results from three methods were taken into account: $e^- + \mu^- + OIS$. In addition, this compilation contained an updated table of radius differences from $K_z IS$. Since then, several experimental results have been published mainly containing $\delta \langle r^2 \rangle$ values from OIS along isotopic series.

Table 1 of the present paper contains rms radius data for 799 isotopes of 91 elements making use of results from the four methods: $e^- + \mu^- + K_z IS + OIS$. Whenever possible, advantage was taken of constraints between directly measured radii and differences. Often, easy-to-use radius formulae with limited number of parameters are required, for example, for the extrapolation of the radius surface $R(N, Z)$ or $R(A, I)$ to unknown regions. In order to facilitate the global description of the smooth surface, simple empirical formulae were fitted to the resulting radius data (see Section 3 and Tables 2 and 3). These formulae may be useful to estimate the values of unmeasured radii, and especially in extrapolating charge radius values for nuclei far from the valley of stability or to perform analytic calculations with the continuous function $R(N, Z)$. A simple two-component liquid-drop model is applied for the interpretation of the empirical results. Finally, in Section 4 a short survey on the fine structure is given.

2. Sources and treatment of data

First, $\langle r^2 \rangle^{1/2}$ data were obtained from e^- and μ^- measurements (from now on, the shorthand notation $R \equiv \langle r^2 \rangle^{1/2}$ is used). Then, differences δR between non-isotope pairs were taken into account. These improve

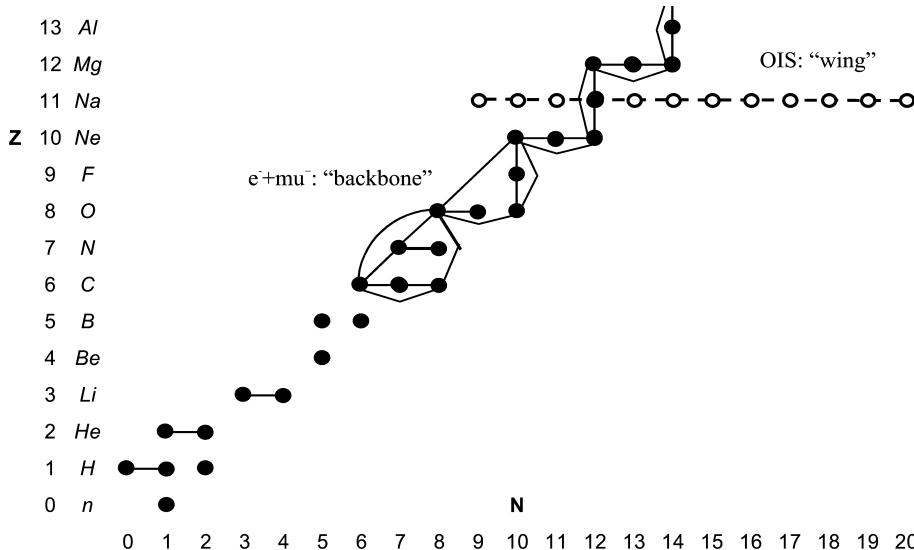


Fig. 1. Illustration of measured quantities and the links between them. Filled circles denote experimental rms radius data, continuous lines mark radius differences measured by electron scattering or muonic atom X-rays. These links are used as constraints to improve the input data and to search for inconsistencies (see Section 2). Broken lines denote differences from optical isotope shifts.

the links between different isotopic series, helping the study of isotonic and isobaric behavior. Then isotopic differences δR measured by e^- and μ^- were taken into account, followed by δR from $K_{\alpha}IS$. Finally, δR values from OIS are included in two steps: (1) differences between isotopes for which there exist data from the previous steps; these altogether form a backbone for the data system in the (N, Z) plot, Fig. 1, and (2) the remaining differences δR constitute the wings that are adjusted to the backbone. Some details of this multi-step task have been published in previous papers, which will be cited in the respective sections (Table 4).

2.1. rms radii from e^- and μ^-

In addition to the compilations, original papers and personal communications have also been taken into account up to January 2004. Of outstanding importance is the compilation [10]. It contains precise rms radius data evaluated model independently by combining e^- , μ^- , and OIS. The sources and treatment of data have been described in [11,12] together with a list of the references, e^- : 316, μ^- : 145. Therefore, this pre-1999 reference list for e^- , μ^- is not repeated here.

At this point, some remarks on the radius data for the proton and deuteron are appropriate. Worldwide data on elastic (el) electron–proton scattering have been re-analyzed taking into account corrections for Coulomb distortion and higher moments, resulting in an rms charge radius $R_{p,el} = 0.895(18)$ fm [13]. The evaluation of high accuracy data of the $1S$ Lamb shift (LS) in hydrogen yielded $R_{p,LS} = 0.883(14)$ fm [14]. The weighted average (av) of these two independent data is $R_{p,av} = 0.887(11)$ fm. For the deuteron, the analysis of world data on elec-

tron scattering resulted in $R_{d,el} = 2.130(12)$ fm [15]. From the measurement of the hydrogen–deuterium isotope shift, the difference of deuteron–proton rms charge radii have been derived: $R_d^2 - R_p^2 = 3.8212(15)$ fm² [16]. Using this as a constraint between $R_{p,av}$ and $R_{d,el}$ in a weighted least-squares adjustment procedure, we have $R_p = 0.8791(88)$ fm and $R_d = 2.1402(91)$ fm as listed in Table 1.

The final database selected contains 460 radius values (from the 1367 data published) for 285 nuclides. In some cases, the error estimates did not contain all components of uncertainty, e.g., model dependence, nuclear polarization correction, etc. In these cases a further error component was added, estimated after reading the respective literature. Quite often, there are several measured radius values for the same nucleus. To find the average value R_{av} and its uncertainty ΔR_{av} of a data group, two different methods were used, an iteration procedure and a single-step one [11]. The results are more sensitive to the decision of which data are included in the procedure, and less sensitive to the way in which the individual data are weighted to form an average. The resulting data system contains 285 isotopes of 85 elements.

2.2. Differences of rms radii from e^- and μ^- (not isotopes)

There are 94 data for 91 pairs of nuclei [7,10,17–20]; some data are from e^- , others from μ^- , while most of them result from a simultaneous evaluation $e^- + \mu^-$. Results of μ^- measurements are often published as Barrett moment [21] differences δR_B . Then the relationship [22]

$$\delta R = v(Z) \sqrt{\frac{3}{5}} \delta R_B, \quad v(Z) = 1 + 0.0035 \times \ln(0.22 \times Z + 1) \quad (1)$$

was applied to derive the rms radius difference δR , where $Z = (Z_1 + Z_2)/2$. In the deformed region the coefficient $v(Z)$ is somewhat modified: $v(Z)_{\text{def}} = v(Z) + 0.00054 \times \min(Z - 60, 77 - Z)$.

2.3. Application of constraints

In several cases, there are redundant, independently measured differences in a group of δR data, that is, in addition to $\delta R_{12}(\pm \Delta \delta R_{12})$ and $\delta R_{23}(\pm \Delta \delta R_{23})$ the radius difference $\delta R_{13}(\pm \Delta \delta R_{13})$ is also measured, e.g., ^{12}C – ^{14}N , ^{14}N – ^{16}O , and ^{12}C – ^{16}O . In these cases the relation $\delta R_{13}^0 = \delta R_{12}^0 + \delta R_{23}^0$ between the true values δR_{ik}^0 can be exploited to improve the accuracy. To do this, the method of weighted least-squares was used. This also made it possible to check the internal consistency of the data group by a χ^2/n' test. The new errors are less than the original ones, being always the least precise measurement that benefits most of the constraint. Some μ^- data groups have already been conditioned during the evaluation of the experiment and so published. Naturally, for these groups the above procedure was not applied. Constraints of the type $R_2^0 = R_1^0 + \delta R_{12}^0$ were also applied.

2.4. Radius differences between isotopes from e^- and μ^-

The main source for δR data between isotopes from electron scattering was the compilation [7], but original papers were also taken into account. There are altogether 88 δR values for 66 isotope pairs. From multiple data a weighted average was formed. For δR values from muonic X-rays the main source was [10], but results from original papers were also included. Resulting in altogether 195 data for 184 isotope pairs. Most of these data are Barrett differences, so they had to be transformed to rms differences making use of Eq. (1).

2.5. Radius differences between isotopes from K_α isotope shifts

Most of the 89 $K_\alpha IS$ data are from Table II of [10], which is an extended version of [2]. Original papers have also been taken into account [23–25]. Two modifications were performed in Table II of [10]: (1) for uranium the correct mass interval is 233 – ^{238}U instead of 235 – ^{238}U , see [26] and (2) regarding the results of a χ^2/n' test [27], the shift for 121 – ^{123}Sb [28] was omitted and some error estimates increased. In the tables energy shifts δE_{Coul} are given, which can be expressed in terms of even moments of the charge distribution: $\delta E_{\text{Coul}} = C_1 \lambda$, where the nuclear parameter

$$\lambda = \delta \langle r^2 \rangle + \frac{C_2}{C_1} \delta \langle r^4 \rangle + \frac{C_3}{C_1} \delta \langle r^6 \rangle + \dots \quad (2)$$

contains information on the size of the nucleus. Seltzer [29] calculated the coefficients C_1 , C_2 , and C_3 . The ratios C_2/C_1 and C_3/C_1 have also been calculated by [30,31]. Dividing the measured energy shift δE_{Coul} by C_1 , one arrives at λ that contains the rms radius difference. Although a plot of λ_{KIS} from $K_\alpha IS$ against $\lambda_{e\mu}$ values formed from e^- and μ^- shows a linear correlation for three isotope pairs of Pb (Fig. 1 of [10]), the validity of $C_1(Z)$ has not been tested experimentally for a wide range of atomic numbers. By 2000, the wealth of δR data from e^- and μ^- experiments made it possible to compare the C_1 value to experiment. In [27] 54 energy shifts δE_{Coul} of 18 elements and the respective radius differences δR from e^- and μ^- are used to determine the experimental coefficients $C_{1,\text{exp}} = \delta E_{\text{Coul}}/\lambda_{e\mu}$ in the atomic number interval $Z = 42$ –92. These experimental coefficients were then compared to the theoretically calculated C_1 values by a $\chi^2(f)$ minimization analysis, where $C_{1,\text{exp}} = f \times C_1$. The result is $f = 0.965(14)$, i.e., the experimental $C_{1,\text{exp}}$ values are, on the average, 3.5% lower than those calculated by Seltzer. It would be most desirable to have a new, more recent calculation of the momentum coefficients C_1 , C_2 , and C_3 with up-to-date theoretical methods.

Applying now the modified Seltzer coefficients $C'_1 = f \cdot C_1$ ($f = 0.965$), we have the modified nuclear parameter $\lambda' = \lambda/f$, from which the difference of mean square radii can be determined by a rapidly converging iteration procedure. Starting with $\delta \langle r^2 \rangle_0 = \lambda'$,

$$\begin{aligned} \delta \langle r^2 \rangle_{i+1} &= \lambda' - \frac{C_2}{C_1} \left[a_4 (\delta \langle r^2 \rangle_i)^2 + b_4 \delta \langle r^2 \rangle_i \right] \\ &\quad - \frac{C_3}{C_1} \left[a_6 (\delta \langle r^2 \rangle_i)^3 + b_6 (\delta \langle r^2 \rangle_i)^2 + c_6 \delta \langle r^2 \rangle_i \right], \end{aligned} \quad (3)$$

where

$$\begin{aligned} a_4 &\equiv \frac{25}{14} \left(\frac{A_2 + A_1}{A_2 - A_1} \right), \quad b_4 \equiv \frac{30}{7} (\pi a)^2, \\ a_6 &\equiv \frac{125}{48} \left(\frac{A_2 + A_1}{A_2 - A_1} \right)^2, \quad b_6 \equiv \frac{275}{18} (\pi a)^2 \left(\frac{A_2 + A_1}{A_2 - A_1} \right), \\ c_6 &\equiv \frac{239}{9} (\pi a)^4 \end{aligned}$$

refer to a Fermi distribution with a constant surface diffuseness $a = t/(4 \ln 3)$ and a mass number dependence $c = r_0 A^{1/3}$ for the half-density radius c . Note that the value of c and r_0 does not appear in the expressions.

2.6. Radius differences from optical isotope shifts

The sources of λ or $\delta \langle r^2 \rangle$ data published before 1989 are the compilations [6,8]. More recent results are taken from original papers, they are listed among the references. Not

all of the data are included in the table. Preference was given to long, recently measured isotopic series. Sometimes, however, results from two different measurements had to be merged. Wherever possible, relative (experimental) and total (experimental + systematic) errors were separately treated. This is because the main motivation of the present work was the investigation of the radius surface $R(N, Z)$. This necessitates the knowledge of absolute radii R . The procedure for the determination of λ and $\delta\langle r^2 \rangle$ values from the measured $\delta\nu$ frequency shifts is described in detail in [6,10,32], together with the limitations of the procedure. Here only the main steps will be recalled. The isotope shift consists of a mass shift and a field (or volume) shift: $\delta\nu = \delta\nu_{MS} + \delta\nu_{FS}$. The latter term can be written in the form $\delta\nu_{FS} = F\lambda$, where the nuclear parameter λ has the same form as in the case of K_zIS (Eq. (2)). Although the values of $C_{i,\text{Opt}}$ for optical transitions are an order of magnitude less than those $C_{i,K}$ for K_z , the corresponding ratios are practically equal: $C_{2,\text{Opt}}/C_{1,\text{Opt}} \approx C_{2,K}/C_{1,K}$ and $C_{3,\text{Opt}}/C_{1,\text{Opt}} \approx C_{3,K}/C_{1,K}$. Therefore, the iteration procedure described above can be utilized for those OIS results, where only λ values are given. In [8] and in some recent papers the measurements have already been evaluated by the so-called two-parameter model [33,34]. These $\delta\langle r^2 \rangle$ values were accepted without changes. A comparison of the two procedures (Table I of [35]) shows that the results are close to each other, the difference being an order of magnitude less than the total error. Radius differences $\delta R \equiv \delta\langle r^2 \rangle^{1/2}$ were calculated from $\delta\langle r^2 \rangle$ by the relation $\delta R = \delta\langle r^2 \rangle/(R_1 + R_2)$. For nuclei where no data for R_1 and R_2 existed, but there were R values for the neighbors on both sides, linear interpolation was used to estimate the missing radius. In the case of isotopic chains, the relation [36,37]

$$R(A) = R(A_0) \times \left(\frac{A}{A_0} \right)^{1/5} \quad (4)$$

was applied for extrapolation from the stable nucleus with mass number A_0 . For the elements Re, Po, Rn, Fr, Ra, and Cm there are no measured R values. In these cases, $R(A_0)$ was estimated by the expression [38]

$$R(A_0) = \left(r_0 + \frac{r_1}{A_0^{2/3}} + \frac{r_2}{A_0^{4/3}} \right) \times A_0^{1/3} \quad (5)$$

with $r_0 = 0.891(2)$ fm, $r_1 = 1.52(3)$ fm, and $r_2 = -2.8(1)$ fm. Note that these elements are used in Section 3 only for the investigation of relative $R_Z(N)$ dependence, but they were omitted while investigating the $R_N(Z)$ and $R_A(I)$ dependence, which necessitated the knowledge of absolute R values.

2.7. Adjusting OIS to $e^- + \mu^- + K_zIS$

The systematic errors arising from specific mass shift and electron factors can be reduced if δR values from other experimental methods are also available. Therefore,

weighted averages $\delta R_{e\mu KO}$ were formed. In doing this, total errors $\Delta\delta R_{O,\text{tot}}$ were used. The uncertainty $\Delta\delta R_{e\mu KO}$ is significantly less than the original $\Delta\delta R_{O,\text{tot}}$. The reduction varies from element to element between 0.2 and 0.6. Using these improved rms differences $\delta R_{e\mu KO}$ and the respective absolute $R_{e\mu}$ radii, 32 data triplets ($2R, 1\delta R$) and 63 quintets ($3R, 2\delta R$) could be formed, and the respective constraints applied. This further improved the accuracy and rendered it possible to correct three inconsistencies. As a result, we have R and δR values that contain in a consistent way all of the experimental information from the four methods. These nuclei constitute the backbone along the valley of stability, onto which the wings, the isotopic series of δR values from OIS , will be fitted.

2.8. Fitting δR_{OIS} series to the backbone

As described in the foregoing, $\delta R_{e\mu KO}$ values were formed for those isotope pairs for which at least two of the four methods were available. Relating the $\delta R_{e\mu KO}$ differences to those measured by OIS , correction factors $\delta R_{e\mu KO}/\delta R_{OIS}$ were formed, their values varied between 0.9 and 1.3. These factors were used to correct those δR_{OIS} differences for which only OIS measurements were available, thus correcting for the eventual common systematic error factor. The corrected δR_{OIS} differences, i.e., the wings were added to the respective backbone R values obtained in the previous paragraph. In this way a set of rms charge radii was obtained, displayed in Table 1. As the correction factor has the same value for the element, this correction does not change the relative trend of $R_Z(N)$ isotopic dependence. However, it improves the absolute R values, which are important for the investigation of the radius surface $R(N, Z)$.

3. Properties of the radius surface $R(N, Z)$

The set of data in Table 1 allows one to investigate the properties of the radius surface $R(N, Z)$ or $R(A, I)$. It is practical to consider this complicated set of points as the superposition of two structures: a smooth, slowly varying surface describing the global or rough structure, and a fine structure having valleys near magic nucleon numbers and mountains at deformations; odd–even staggering is also observed. The shell and deformation dependence has long been investigated [9,37,39–42]. On the other hand, the slow variations almost escaped attention, in spite of the fact that it may be a useful tool for extrapolation of R values to the limits of nucleon stability.

3.1. Global behavior of the radius surface along the valley of stability

First, following tradition, the mass number dependence along the valley of stability is examined using 299

isotopes of 74 elements. The radius parameter r_{LD} of the well-known liquid-drop (LD) model [43]

$$R_{LD} = r_{LD} A^{1/3} \quad (6)$$

was determined by a minimum- χ^2 procedure. The result is shown in Table 2 together with the standard deviation and the reduced χ^2 value χ^2/n' . It is interesting to see that the purely empirical function

$$R_e = r_e A^e \quad (7)$$

has its best fit with an exponent value $e = 0.294(1)$, which significantly differs from 1/3. Taking into account the finite surface thickness, Elton [44] derived a three-parameter formula

$$R_s = \left(r_0 + \frac{r_1}{A^{2/3}} + \frac{r_2}{A^{4/3}} \right) \times A^{1/3}, \quad (8)$$

which yields a better fit to the data. During the work it was found that the parameters r_1 and r_2 are strongly anticorrelated, which can be described by the simple linear relation $r_2 \approx -(1.4r_1 - 1)$. Hence, there remain only two free parameters in Eq. (8).

3.2. Intersections of the radius surface

The properties of the radius surface can be investigated by studying its different intersections by planes perpendicular to the (N, Z) plane, namely the $R_Z(N)$, $R_N(Z)$, and $R_A(I)$ dependencies. As the latter is redundant information, its result can be used to apply a constraint with the former two. Finally, the direction $\Delta Z/\Delta N$, for which $R(N, Z) \approx \text{constant}$, is determined. For isotopic chains the radius formula

$$R_Z(N) = R_0 \left(\frac{A}{A_0} \right)^{k_Z}, \quad A = A_0 + \Delta N \quad (9)$$

was applied, where R_0 is the rms charge radius of the reference isotope (Z, A_0) . Results of a weighted least-squares fit (k_Z , standard deviation (SD) and χ^2/n') are indicated in Table 3 under the column “From experiment.” The procedure was also performed separately for proton-rich and neutron-rich nuclei. The Z -dependence along isotonic series was investigated by fitting the formula

$$R_N(Z) = R_0 \left(\frac{A}{A_0} \right)^{k_N}, \quad A = A_0 + \Delta Z. \quad (10)$$

The resulting value of the parameter k_N is shown in Table 3. The simplified neutron and proton number dependence is illustrated schematically in Fig. 2, using rounded values of the exponents. It follows that the smooth component of the radius surface, around the nuclid $A_0 = Z_0 + N_0$, can be described by

$$\begin{aligned} R(N, Z) &= R_0 \left(\frac{Z_0 + N}{A_0} \right)^{k_Z} \left(\frac{Z + N}{Z_0 + N} \right)^{k_N} \\ &\approx R_0 \left(1 + \frac{\Delta N}{A_0} \right)^{k_Z} \left(1 + \frac{\Delta Z}{A_0} \right)^{k_N}, \end{aligned} \quad (11)$$

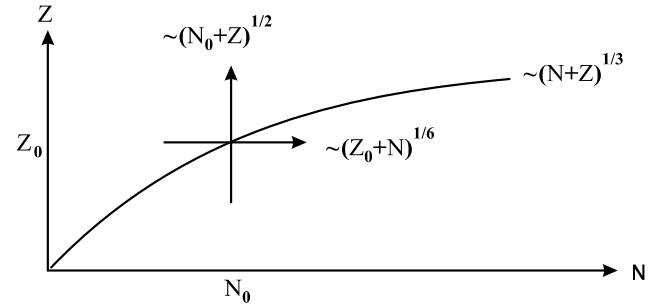


Fig. 2. Schematic illustration of the smooth radius surface $R(N, Z)$ around a reference nuclide $R(N_0, Z_0)$ (see Eqs. (9) and (10)). The exponents are rounded values of the empirical parameters shown in Table 3.

where $R_0 \equiv R(N_0, Z_0)$, $\Delta Z \equiv Z - Z_0$, and $\Delta N \equiv N - N_0 \ll N$.

Next, referring to Fig. 3, the surface $R(N, Z)$ can be represented by the level lines corresponding to rms radii with intervals $\Delta R = 0.5 \text{ fm}$ (Fig. 3B). For comparison, contour lines of the liquid-drop formula, Eq. (6) are plotted in Fig. 3A.

Along isobaric series the dependence of rms radii on the symmetry parameter $I \equiv (N - Z)/A$ was studied by $R_A(I) = R_0[1 + f(I - I_0)]$, $I_0 \equiv (N_0 - Z_0)/A$. (12)

The results for f are also shown in Table 3. They are close to those published earlier [45,46]. The search for the level lines $R(N, Z) = \text{constant}$ was performed considering a formula similar to those above

$$R_L(\Delta N, \Delta Z) = R_0 \left(\frac{A}{A_0} \right)^{k_{CR}} \quad (13)$$

(k_{CR} is the parameter for constant radius) but it was used in a different way; during the fits the $|k_{CR}| \approx 0$ value was sought by choosing different directions in the (N, Z) plane. A direction can be characterized by the slope $\Delta Z/\Delta N$, and also by the value of the invariant L . For example, nuclei on the line with slope $(\Delta Z/\Delta N) = -(1/3)$ are characterized by $L = 3Z + N = \text{constant}$ as $^{20}_{11}\text{N}-^{22}_{10}\text{Ne}$. This means that, on the average, a decrease of rms charge radius caused by picking out a proton from the nucleus can be compensated by adding three neutrons to it.

3.3. Application of constraints between the empirical parameters

Having these experimental parameters, their values can be improved by using the relations between them.

1. Starting from $A_0 = N_0 + Z_0$ one can arrive at the isobar $A = N + Z = A_0$ by the isotopic chain of element Z_0 through $A_1(N, Z_0)$ followed by the isotonic series containing N neutrons. Alternatively, one can step directly from (N_0, Z_0) to (N, Z) by varying the symmetry

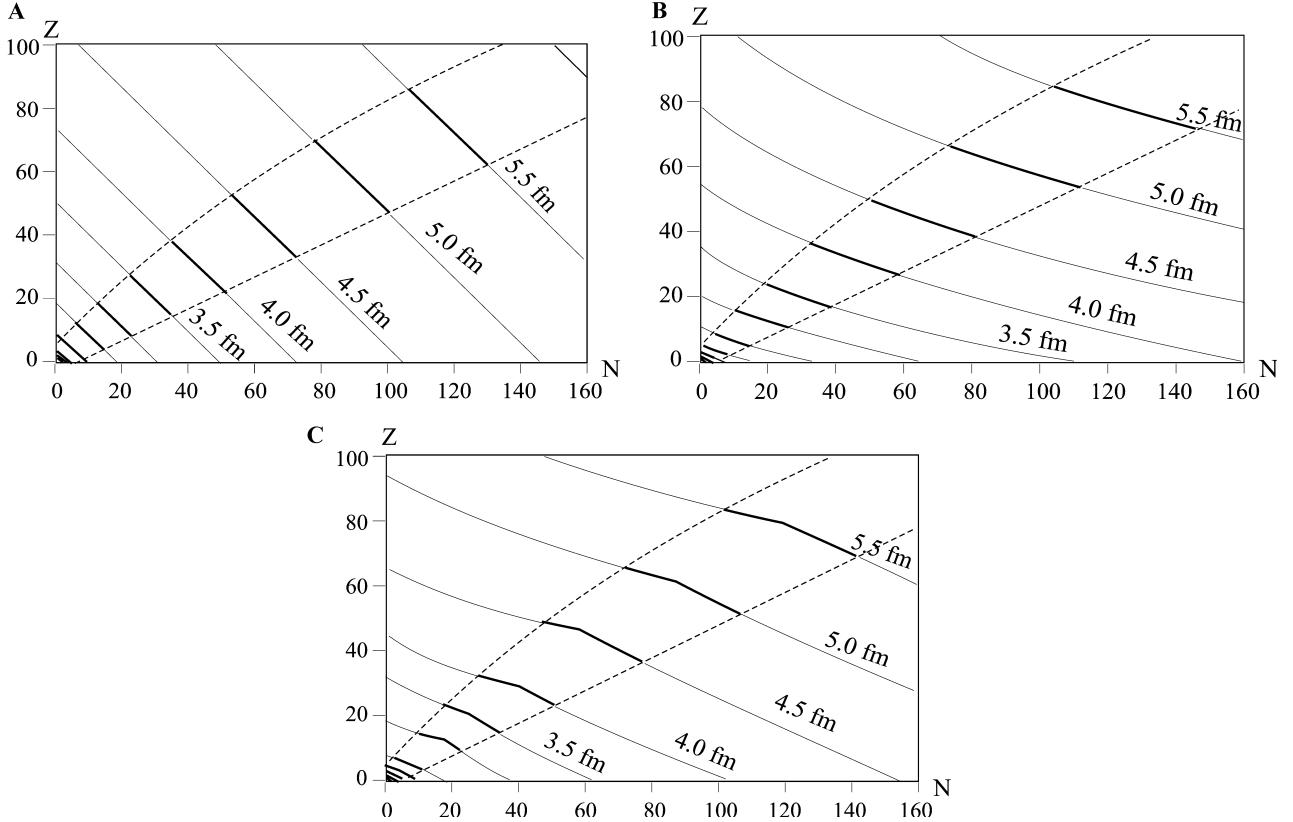


Fig. 3. (A) Level lines of the surface described by the liquid-drop model, Eq. (6) of Section 3. Broken lines show the region of nucleon stability. (B) Level lines of the surface described by the empirical formulae Eqs. (9) and (10) in Section 3. The slope -0.33 means that a decrease in R caused by removing a proton from the nucleus can be compensated by adding three neutrons to it. Broken lines show the region of nucleon stability. (C) Same as (B) but with separate parameter values for proton-rich and for neutron-rich nuclei (see Table 3). The indentation on the radius surface along the line of stability is clearly seen (see also Section 3).

parameter I . It can be shown that the relation for the true values of the parameters

$$f^0 \approx \frac{1}{2}(k_Z^0 - k_N^0) \quad (14)$$

is valid to a good approximation. The systematic error of this approximation ($\leq 1\%$) is much less than the experimental uncertainties of the parameters. The results for k_Z , k_N , and f derived by this constraint are shown in the last column of Table 3.

2. It can also be shown that for nuclei along iso-radius series ($R \approx \text{constant}$) the ratio $-k_Z/k_N$ is close to the slope $\Delta Z/\Delta N$. Therefore, this ratio can be regarded as an independent estimation of the slope. Here, the systematic error of the approximation ($\sim 10\%$) is about the same size as the experimental one. This is taken into account by choosing the weights accordingly. Then the weighted average of $-k_Z/k_N$ and $\Delta Z/\Delta N$ was formed. These are shown for $\Delta Z/\Delta N$ in the last column of Table 3.

3.4. The two-liquid drop model

The smooth behavior of the radius surface renders its interpretation possible by a simple model, which is a

simple extension of the traditional liquid-drop approach. Here only the main characteristics and results are described and details will be published elsewhere. The model works with uniform density distributions (by sections) for protons and neutrons separately. Their sum $\rho_0 = \rho_P + \rho_N$ is assumed constant within a radius $R_0 = (3A/4\pi\rho_0)^{1/3}$. In the calculations an average nucleon density $\rho_0 = 0.128 \text{ n}/\text{fm}^{-3}$ was used, as obtained from fitting the liquid-drop formula (6) to stable nuclei. (The value $\rho_{0,F} \approx 0.17 \text{ n}/\text{fm}^{-3}$, as often found in the literature, refers to the maximum density of a Fermi-like distribution fitted to measurements on the heaviest nuclei [44, p. 50].) It is assumed that in stable nuclei $\rho_{P,st}$ and $\rho_{N,st}$ both extend to R_0 . Away from stability the extension and ratio of ρ_P and ρ_N are different. In proton-rich nuclei there is a proton skin from R_N to R_0 ; in neutron-rich nuclei there is a neutron skin from R_p to R_0 . In the case of tin isotopes, rms radius values calculated by the model and by Eq. (9) are close to each other, the standard deviation being $SD = 0.004 \text{ fm}$. The skin thickness formed by the majority nucleons depends almost linearly on $dA \equiv A - A_{\text{stab}}$: $dR = 0.008 \times dA$. Here the skin thickness dR is defined naturally as the difference between the radius parameters of the model, while

most experiments generally yield the difference of rms neutron and proton radii. For uniform density distributions with radius difference dR_{np} the simple relation holds: $d\langle r^2 \rangle_{np}^{1/2} = \sqrt{3/5} dR_{np}$. It should be noted that in the present simple form of the model it was postulated that at the line of stability the proton and neutron densities have the same radius, the skin thickness vanishes. This may not be true. There is evidence for a finite neutron skin, e.g. [47].

Small differences between the model and the empirical formula (9) suggested that different values for the empirical parameters should be used for proton-rich and neutron-rich nuclei, respectively. Results of these parameter searches are shown in Table 3. The level lines of the surface $R(N, Z)$ calculated with these parameters are plotted in Fig. 3C. It seems that there is an indentation in the radius surface along the stability line.

A possible interpretation for the indentation may be a decrease in ρ_0 as one moves away from the line of stability. Assuming a linear dependence on $|I - I_{st}|$, the nuclear density $\rho_0 = \rho_{0,st}(1 + g|I - I_{st}|)$ was introduced into the model by varying the value of the parameter g , so that the minimum SD was searched. In the case of the $Z = 50$ isotopic series the result is $g = -0.12$ ($SD = 0.0021$). That is, going away from the line of stability to $|I - I_{st}| = 0.1$, e.g., from $A = 118$ to 105, the density ρ_0 decreases by 1%.

4. Fine structure in the charge radii

Along the valley of stability radii of nuclei near or at magic nucleon numbers are significantly less than the average trend, while they deviate upwards in between. These deviations can be described by the nucleonic promiscuity factor [48] $P \equiv N_p N_n / (N_p + N_n)$ in the formula [45]

$$R_p = R_{0,p} + dR_p \\ = \left(r_{0,p} + \frac{r_{1,p}}{A^{2/3}} + \frac{r_{2,p}}{A^{4/3}} \right) \times A^{1/3} + a \frac{P}{R_{0,p}} \quad (15)$$

where $R_{0,p}$ is the radius for closed-shell nuclei, while N_p and N_n are numbers of valence protons and neutrons (or holes), respectively. Values of the parameters $r_{0,p}$, $r_{1,p}$, $r_{2,p}$, and a are shown in Table 2. For the calculation of the factor P the following magic numbers produced the best fit: $Z_M = 2, 6, 14, 28, 50, 82, (114)$, and $N_M = 2, 8, 14, 28, 50, 82, 126, (184)$. It should be noted that in other investigations [42,49,50], too, the irregular magic numbers 6 and 14 proved to be present. Other semi-magic proton and neutron numbers at $Z_M = 40, 64$ and $N_M = 56$ [51] were also tested in several combinations but without positive result. The parameters of the formula vary somewhat with mass number; therefore, the

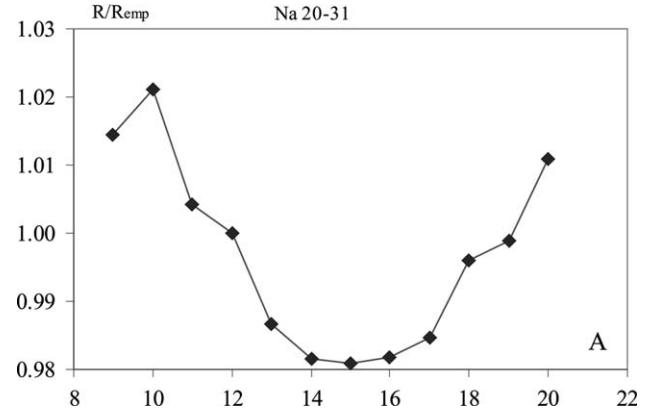


Fig. 4. R/R_{emp} values for sodium isotopes. R , Experimental rms charge radii from [52]; R_{emp} , radii calculated by the empirical formula Eq. (9) in Section 3.

parameter set for light nuclei 9Be – ${}^{27}Al$ is separately given in Table 2.

Along isotopic series the smooth function $R(N, Z)$ may be used to divide the individual experimental R values. The resulting R/R_{emp} values (where R_{emp} is the value of the smooth empirical function for the given nucleus) along isotopic series follow nearly the same systematics as observed earlier [9,37,39–42], showing pronounced shell effects for neutron numbers $N = 28, 50, 82$, and 126 . In the case of light nuclei $N \sim 14$ – 16 they seem to have magic character (see Fig. 4 regarding experimental data from [52]). (Figures for other elements can be obtained from the author.) A sudden increase at the transitional region $N \sim 88$ – 90 can also be clearly observed. Isotonic series are less accurate, but the main shell effects at $Z = 28, 50$, and 82 are clearly noticeable.

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References

- [1] R. Hofstadter, H.R. Collard, in: H. Schopper (Ed.), Landolt-Börnstein, New series, Group I. Nuclear Physics and Technology, vol. 2, Nuclear Radii, Springer-Verlag, Berlin, 1967.
- [2] F. Boehm, P.L. Lee, At. Data Nucl. Data Tables 14 (1974) 605.
- [3] R. Engfer et al., At. Data Nucl. Data Tables 14 (1974) 509.
- [4] K. Heilig, A. Steudel, At. Data Nucl. Data Tables 14 (1974) 613.
- [5] C.W. deJager et al., At. Data Nucl. Data Tables 14 (1974) 479.
- [6] P. Aufmuth et al., At. Data Nucl. Data Tables 37 (1987) 455.
- [7] H. deVries et al., At. Data Nucl. Data Tables 36 (1987) 495.
- [8] E.W. Otten, in: Treatise in Heavy-Ion Physics, vol. 8, 1989, p. 604.

- [9] E.G. Nadjakov et al., At. Data Nucl. Data Tables 56 (1994) 133.
- [10] G. Fricke et al., At. Data Nucl. Data Tables 60 (1995) 177.
- [11] I. Angeli, Acta Phys. Hung. 69 (1991) 233.
- [12] I. Angeli, Table of Nuclear Root Mean Square Charge Radii, INDC(HUN)-033, September 1999 (IAEA Nuclear Data Section, Vienna). Available from <<http://www.nds.iaea.or.at/indc-sel.html>>.
- [13] I. Sick, Phys. Lett. B 576 (2003) 62.
- [14] K. Melnikov, T. van Ritbergen, Phys. Rev. Lett. 84 (2002) 1673.
- [15] I. Sick, D. Trautmann, Nucl. Phys. A 637 (1998) 559.
- [16] A. Huber et al., Phys. Rev. Lett. 80 (1998) 468.
- [17] H.D. Wohlfahrt et al., Phys. Rev. C 22 (1980) 264.
- [18] H.D. Wohlfahrt et al., Phys. Rev. C 23 (1981) 533.
- [19] J. Herberz, Ph.D. thesis, University of Mainz, KPH 6/89 (1989).
- [20] G. Fricke et al., Phys. Rev. C 45 (1992) 80.
- [21] R.C. Barrett, Phys. Lett. B 33 (1970) 388.
- [22] I. Angeli, Acta Phys. Hung. New Series 15 (2002) 87.
- [23] P.L. Lee, F. Boehm, A.A. Hahn, Phys. Rev. C 17 (1978) 1859.
- [24] C.W.E. Eijk et al., J. Phys. G 5 (1979) 315.
- [25] S.R. Elliott et al., Phys. Rev. Lett. 76 (1996) 1031.
- [26] R.T. Brockmeier et al., Phys. Rev. Lett. 15 (1965) 132.
- [27] I. Angeli, Hyperfine Interact. 136 (2001) 17.
- [28] A.S. Rybníkář et al., J. Exp. Theor. Phys. 63 (1972) 53.
- [29] E.C. Seltzer, Phys. Rev. 188 (1969) 1916.
- [30] G. Torbohm et al., Phys. Rev. A 31 (1985) 2038.
- [31] S.A. Blundell et al., J. Phys. B 20 (1987) 3663.
- [32] K. Heilig, Hyperfine Interact. 38 (1987) 803.
- [33] S.A. Ahmad et al., Z. Phys. A 321 (1985) 35.
- [34] S.A. Ahmad et al., Nucl. Phys. A 483 (1988) 244.
- [35] I. Angeli, Acta Phys. Hung. New Series 17 (2003) 3.
- [36] J.P. Schiffer, Phys. Lett. 29B (1969) 399.
- [37] I. Angeli, M. Csatlós, Nucl. Phys. A 288 (1977) 480.
- [38] I. Angeli, AMCO-9, in: 9th Conference on Atomic Masses and Fundamental Constants, July 19–24, 1992, Bernkastel-Kues.
- [39] D.N. Stacey, Rep. Prog. Phys. 29 (1966) 171.
- [40] I. Angeli, M. Csatlós, ATOMKI Közlemények 20 (1978) 1.
- [41] W.D. Myers, K.H. Schmidt, Nucl. Phys. A 410 (1983) 61.
- [42] E. Wesolowski, J. Phys. G. 11 (1985) 909.
- [43] G. Gamow, Proc. R. Soc. Lond. A 216 (1930) 632.
- [44] L.R.B. Elton, Nuclear Sizes, Oxford University Press, Oxford, 1961.
- [45] I. Angeli, J. Phys. G. 17 (1991) 439.
- [46] I. Angeli, Acta Phys. Hung. New Series 13 (2001) 149.
- [47] A. Krasznahorkay et al., Phys. Rev. Lett. 82 (1999) 3216.
- [48] R.F. Casten et al., Phys. Rev. Lett. 58 (1987) 65.
- [49] M. Uno, M. Yamada, Progr. Theor. Phys. 53 (1975) 987.
- [50] M. Uno, M. Yamada, Progr. Theor. Phys. 65 (1981) 1322.
- [51] N. Zeldes, in: P.G. Hansen, O.B. Nielsen (Eds.), Proceedings of the 4th International Conference on Nuclei Far From Stability, vol. I, Geneva, CERN, 1981, p. 93.
- [52] F. Touchard et al., Phys. Rev. C 25 (1982) 2756.

Explanation of Tables

Table 1. Nuclear rms charge radii

<i>Z</i>	Atomic (proton) number of the element
<i>El</i>	Chemical symbol of the element
(El)	For six elements, designated by parentheses (El) there are only δR measurements; the reference R_0 values were estimated by Eq. (5)
<i>A</i>	Mass number of the isotope
<i>R</i> (fm)	$\equiv \langle r^2 \rangle^{1/2}$. Experimental root-mean-square charge radius in fm = 10^{-15} m. For the neutron $\langle r^2 \rangle$ is given in fm ² . For the proton, see also paragraph 3 in Section 2.
$\Delta_{\text{tot}}R$ (fm)	Total error of <i>R</i> , including both experimental and systematic errors, in fm = 10^{-15} m. See Section 2
$\Delta_{\text{rel}}R$ (fm)	Relative error of <i>R</i> with respect to the radius of the reference isotope; in fm = 10^{-15} m. See Section 2

Table 2. Parameters of radius formulae for nuclei near the stability line

Model	Model underlying the radius formula
Equation	Number of the equation of the radius formula in Section 1
Parameters	Best-fit parameter values of the formula
St. Dev. (fm)	Standard deviation of the experimental data from the formula
χ^2/n'	Reduced χ^2 value

Table 3. Empirical parameters characterizing the radius surface $R(N, Z)$

Equation	Number of the empirical formula
Parameter	Parameter of the formula
Region	Region of nuclei where the fit was performed
From experiment	Result of the best-fit procedure to the experimental data
St. Dev. (fm)	Standard deviation of the experimental data from the formula
χ^2/n'	Reduced χ^2 value
With constraint	Parameter values improved by the constraints, see Eq. (14) in Section 3.

Table 4. Annotated references for the Introduction and for the Tables

Table 1

Nuclear rms charge radii. (For the neutron the entry is $\langle r^2 \rangle$ (fm 2) and for the proton and deuteron, see Section 2.) See page 194 for Explanation of Tables

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
0	n	1	-0.1149	.0024	
1	H	1	0.8791	.0088	
		2	2.1402	.0091	
		3	1.7591	.0356	
2	He	3	1.9448	.0137	
		4	1.6757	.0026	
3	Li	6	2.5385	.0267	
		7	2.4312	.0281	
4	Be	9	2.5180	.0114	
5	B	10	2.4278	.0492	
		11	2.4059	.0291	
6	C	12	2.4703	.0022	
		13	2.4614	.0033	
		14	2.5037	.0081	
7	N	14	2.5579	.0068	
		15	2.6061	.0074	
8	O	16	2.7013	.0055	
		17	2.6953	.0073	
		18	2.7745	.0058	
9	F	19	2.8976	.0024	
10	Ne	17	3.0428	.0188	.0135
		18	2.9719	.0084	.0048
		19	3.0081	.0053	.0033
		20	3.0053	.0021	
		21	2.9672	.0026	
		22	2.9541	.0019	
		23	2.9126	.0105	.0057
		24	2.9032	.0104	.0044
		25	2.9305	.0133	.0069
		26	2.9268	.0153	.0081
		28	2.9632	.0245	.0159
11	Na	20	2.9716	.0424	.0119
		21	3.0138	.0287	.0084
		22	2.9852	.0169	.0067
		23	2.9936	.0021	
		24	2.9736	.0168	.0067
		25	2.9770	.0249	.0050
		26	2.9928	.0327	.0030
		27	3.0133	.0461	.0066
		28	3.0394	.0573	.0082
		29	3.0915	.0718	.0131
		30	3.1172	.0878	.0195
		31	3.1702	.0891	.0113
12	Mg	24	3.0568	.0017	
		25	3.0280	.0021	
		26	3.0334	.0020	
13	Al	27	3.0605	.0040	
14	Si	28	3.1223	.0024	
		29	3.1168	.0050	
		30	3.1332	.0040	
15	P	31	3.1888	.0018	
16	S	32	3.2608	.0018	
		34	3.2845	.0021	
		36	3.2982	.0021	
17	Cl	35	3.3652	.0145	
		37	3.3840	.0170	
18	Ar	32	3.3462	.0103	.0057
		33	3.3434	.0076	.0031
		34	3.3649	.0043	.0009
		35	3.3632	.0066	.0039
		36	3.3902	.0020	.0006

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
		37	3.3901	.0028	.0013
		38	3.4020	.0017	
		39	3.4085	.0105	.0099
		40	3.4269	.0017	.0006
		46	3.4363	.0068	.0032
19	K	38	3.4262	.0067	.0057
		39	3.4346	.0017	
		40	3.4378	.0027	.0003
		41	3.4514	.0030	.0004
		42	3.4512	.0074	.0020
		43	3.4551	.0089	.0013
		44	3.4558	.0104	.0014
		45	3.4599	.0121	.0017
		46	3.4552	.0129	.0016
		47	3.4529	.0141	.0017
20	Ca	40	3.4764	.0010	
		41	3.4768	.0011	.0004
		42	3.5063	.0010	.0007
		43	3.4928	.0008	.0005
		44	3.5155	.0009	.0009
		45	3.4931	.0015	.0008
		46	3.4925	.0009	.0007
		47	3.4771	.0022	.0019
		48	3.4738	.0009	.0009
		49	3.5145	.0072	.0049
		50	3.5443	.0023	
	Sc	45	3.6052	.0016	.0008
	Ti	46	3.5944	.0018	.0009
		47	3.5912	.0017	
		49	3.5735	.0018	
		50	3.5704	.0016	
	V	51	3.5994	.0022	
	Cr	50	3.6604	.0022	
		52	3.6424	.0021	
		53	3.6588	.0021	
		54	3.6866	.0017	
11	Na	21	3.7057	.0022	
		25	3.6931	.0018	
	Mn	55	3.7371	.0015	
	Fe	54	3.7534	.0017	
		56	3.7748	.0014	
		57	3.7748	.0014	
	Co	59	3.8119	.0014	
	Ni	58	3.8221	.0017	
		60	3.8406	.0016	
		61	3.8587	.0017	
12	Mg	29	3.8823	.0017	
		63	3.9022	.0017	
		65	3.9286	.0014	
13	Al	30	3.9496	.0013	
14	Si	27	3.9665	.0014	
		68	3.9845	.0019	
		70	4.0118	.0018	
		71	4.0414	.0012	
	Ge	72	4.0577	.0012	
		73	4.0634	.0014	
		74	4.0744	.0012	
15	P	31	4.0812	.0012	
16	S	32	4.0969	.0019	
		75	4.0700	.0200	
		76	4.1397	.0016	
		77	4.1397	.0017	

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
35	Br	78	4.1407	.0018	
		80	4.1399	.0019	
		82	4.1399	.0020	
		79	4.1630	.0021	
		81	4.1599	.0021	
		72	4.1635	.0071	.0022
		74	4.1871	.0040	.0006
		75	4.2097	.0041	.0008
		76	4.2020	.0034	.0005
		77	4.2082	.0035	.0006
36	Kr	78	4.2032	.0016	.0004
		79	4.2034	.0029	.0005
		80	4.1976	.0013	.0008
		81	4.1953	.0021	.0005
		82	4.1922	.0015	.0004
		83	4.1860	.0018	.0004
		84	4.1882	.0014	.0001
		85	4.1846	.0014	.0005
		86	4.1836	.0012	
		87	4.1986	.0021	.0004
		88	4.2174	.0040	.0005
		89	4.2290	.0052	.0005
		90	4.2428	.0070	.0012
		91	4.2549	.0080	.0007
		92	4.2732	.0099	.0006
		93	4.2802	.0106	.0005
		94	4.3014	.0128	.0005
		95	4.3078	.0135	.0004
37	Rb	96	4.3282	.0160	.0012
		76	4.2289	.0092	.0033
		77	4.2380	.0084	.0008
		78	4.2410	.0084	.0004
		79	4.2303	.0066	.0003
		80	4.2287	.0065	.0008
		81	4.2225	.0051	.0003
		82	4.2164	.0044	.0008
		83	4.2057	.0026	.0002
		84	4.1992	.0022	.0004
		85	4.2031	.0018	.0003
		86	4.2019	.0020	.0004
		87	4.1981	.0017	
		88	4.2178	.0039	.0010
		89	4.2419	.0073	.0004
		90	4.2599	.0103	.0010
		91	4.2783	.0132	.0007
		92	4.2983	.0164	.0010
38	Sr	93	4.3135	.0189	.0010
		94	4.3287	.0214	.0011
		95	4.3517	.0251	.0013
		96	4.3637	.0271	.0014
		97	4.4458	.0404	.0021
		98	4.4577	.0424	.0022
		78	4.2550	.0040	.0010
		79	4.2577	.0052	.0007
		80	4.2550	.0048	.0008
		81	4.2534	.0041	.0007
		82	4.2457	.0037	.0007
		83	4.2432	.0030	.0005
		84	4.2364	.0017	.0004

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
39	Y	90	4.2606	.0034	.0005
		91	4.2747	.0043	.0004
		92	4.2949	.0059	.0006
		93	4.3062	.0067	.0005
		94	4.3244	.0081	.0007
		95	4.3370	.0090	.0006
		96	4.3612	.0108	.0007
		97	4.3725	.0117	.0009
		98	4.4578	.0178	.0008
		99	4.4710	.0189	.0010
40	Zr	100	4.4874	.0206	.0019
		39	Y	89	4.2417
		40	Zr	87	4.2820
				88	4.2812
				89	4.2715
				90	4.2696
				91	4.2844
				92	4.3057
				94	4.3312
				96	4.3498
41	Nb	97	4.3933	.0091	.0006
		98	4.4185	.0109	.0006
		99	4.4349	.0121	.0006
		100	4.5220	.0184	.0005
		101	4.5487	.0203	.0006
		102	4.5690	.0218	.0006
		95	4.3241	.0015	
		96	4.3156	.0011	
		94	4.3518	.0009	
		95	4.3617	.0009	
42	Mo	96	4.3841	.0008	
		97	4.3877	.0008	
		98	4.4088	.0011	
		100	4.4458	.0013	
		96	4.3927	.0047	
		98	4.4232	.0055	
		99	4.4346	.0042	
		100	4.4536	.0031	
		101	4.4616	.0020	
		102	4.4818	.0018	
43	Ru	104	4.5104	.0020	
		45	Rh	103	4.4942
		46	Pd	102	4.4839
		104	4.5086	.0025	
		105	4.5158	.0025	
		106	4.5322	.0028	
		108	4.5563	.0028	
		110	4.5776	.0031	
		101	4.4712	.0093	.0003
		103	4.4976	.0070	.0002
44	Ag	104	4.5069	.0062	.0002
		105	4.5237	.0049	.0002
		107	4.5442	.0035	.0001
		109	4.5647	.0029	
		102	4.4704	.0095	.0047
		103	4.4860	.0088	.0045
		104	4.5052	.0088	.0051
		105	4.5157	.0071	.0037
		106	4.5340	.0045	.00004
		107	4.5438	.0057	.0032
45	Cd	108	4.5538	.0045	.00003
		109	4.5590	.0063	.0044
		110	4.5743	.0025	.00002
		111	4.5798	.0022	.00002

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
49	In	112	4.5950	.0020	
		113	4.6006	.0020	.00002
		114	4.6137	.0019	
		115	4.6170	.0054	.0049
		116	4.6284	.0021	.00002
		118	4.6316	.0037	.0024
		120	4.6379	.0059	.0045
		104	4.5168	.0119	.0016
		105	4.5298	.0105	.0015
		106	4.5364	.0096	.0013
		107	4.5487	.0082	.0011
		108	4.5566	.0071	.0005
		109	4.5684	.0061	.0008
		110	4.5742	.0056	.0009
		111	4.5859	.0043	.0005
		112	4.5911	.0039	.0007
		113	4.6018	.0025	.00003
		114	4.6066	.0027	.0002
50	Sn	115	4.6169	.0024	
		116	4.6225	.0024	.0001
		117	4.6308	.0030	.0004
		118	4.6353	.0031	.0002
		119	4.6427	.0038	.0004
		120	4.6464	.0040	.0002
		121	4.6527	.0046	.0003
		122	4.6557	.0050	.0004
		123	4.6619	.0055	.0003
		124	4.6650	.0060	.0006
		125	4.6696	.0063	.0005
		126	4.6728	.0068	.0008
		127	4.6761	.0071	.0008
		108	4.5607	.0027	.0004
		109	4.5690	.0025	.0004
		110	4.5807	.0064	.0003
		111	4.5859	.0061	.0003
		112	4.5943	.0018	.0002
		113	4.6038	.0047	.0001
		114	4.6103	.0017	.0003
		115	4.6167	.0038	.0001
51	Sb	116	4.6266	.0015	
		117	4.6318	.0012	.0001
		118	4.6413	.0011	.0001
		119	4.6450	.0010	.0001
		120	4.6543	.0009	.0002
		121	4.6589	.0013	.0001
		122	4.6657	.0010	.0003
		123	4.6684	.0020	.0001
		124	4.6759	.0012	.0004
		125	4.6779	.0027	.0003
52	Te	121	4.6802	.0023	
		123	4.6879	.0021	
		122	4.7084	.0021	
		123	4.7111	.0023	
		124	4.7178	.0017	
53	I	125	4.7198	.0018	
		126	4.7269	.0021	
		128	4.7353	.0025	
		130	4.7426	.0025	
		127	4.7500	.0038	
		116	4.7113	.0084	.0010
		118	4.7318	.0073	.0007
		120	4.7461	.0066	.0007
		122	4.7555	.0061	.0006
		124	4.7621	.0046	.0005

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
55	Cs	126	4.7703	.0048	.0007
		128	4.7755	.0048	.0004
		129	4.7762	.0047	.0001
		130	4.7832	.0046	.0003
		131	4.7812	.0046	.0001
		132	4.7866	.0047	.0002
		134	4.7921	.0047	.0001
		136	4.7991	.0047	
		137	4.8143	.0048	.0003
		138	4.8359	.0054	.0003
		139	4.8511	.0060	.0006
		140	4.8694	.0067	.0002
		141	4.8845	.0075	.0004
		142	4.9016	.0086	.0009
		143	4.9137	.0092	.0004
		144	4.9300	.0102	.0005
		146	4.9575	.0119	.0005
		118	4.7834	.0092	.0002
		119	4.7898	.0090	.0006
56	Ba	120	4.7916	.0076	.0001
		121	4.7773	.0078	.0001
		122	4.7776	.0070	.0002
		123	4.7823	.0070	.0001
		124	4.7831	.0062	.0001
		125	4.7882	.0062	.0001
		126	4.7875	.0056	.0001
		127	4.7938	.0055	.0001
		128	4.7923	.0052	.00004
		129	4.7982	.0051	.0001
54	Xe	130	4.7993	.0049	.0001
		131	4.8026	.0047	.0001
		132	4.8003	.0046	.0001
		133	4.8041	.0046	
		134	4.8031	.0046	.0001
		135	4.8067	.0047	.0001
		136	4.8058	.0052	.0001
		137	4.8126	.0050	.0001
		138	4.8251	.0050	.0001
		139	4.8414	.0069	.0001
51	Sb	140	4.8545	.0088	.0001
		141	4.8678	.0109	.0002
		142	4.8812	.0132	.0001
		143	4.8950	.0151	.0002
		144	4.9039	.0162	.0002
		145	4.9171	.0191	.0002
		146	4.9263	.0193	.0003
		120	4.8088	.0057	.0002
		121	4.8176	.0052	.0002
		122	4.8154	.0053	.0003
52	Te	123	4.8136	.0055	.0003
		124	4.8187	.0051	.0002
		125	4.8179	.0052	.0002
		126	4.8225	.0049	.0002
		127	4.8207	.0050	.0002
		128	4.8260	.0047	.0001
		129	4.8252	.0048	.0001
		130	4.8288	.0047	.0001
		131	4.8281	.0047	.0001
		132	4.8309	.0046	.0001
53	I	133	4.8291	.0046	.0001
		134	4.8298	.0048	.0001
		135	4.8273	.0048	.0001
		136	4.8327	.0048	.0001
		137	4.8326	.0048	.0001
		116	4.7113	.0084	.0010
		118	4.7318	.0073	.0007
		120	4.7461	.0066	.0007
		122	4.7555	.0061	.0006
		124	4.7621	.0046	.0005

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
57	La	138	4.8385	.0045	
		139	4.8523	.0048	.0001
		140	4.8697	.0058	.0001
		141	4.8823	.0068	.0001
		142	4.8973	.0082	.0002
		143	4.9110	.0096	.0002
		144	4.9264	.0112	.0002
		145	4.9375	.0124	.0002
		146	4.9513	.0139	.0002
		148	4.9773	.0168	.0004
		137	4.8492	.0060	.0029
		138	4.8464	.0053	.0011
		139	4.8549	.0049	
58	Ce	136	4.8737	.0017	.0002
		138	4.8735	.0017	.0002
		140	4.8770	.0017	
		142	4.9065	.0017	
		144	4.9308	.0024	.0002
		146	4.9602	.0028	.0002
		148	4.9911	.0035	.0002
		141	4.8919	.0050	
		132	4.9168	.0038	.0029
		134	4.9123	.0031	.0020
59	Pr	135	4.9080	.0040	.0032
		136	4.9106	.0035	.0026
		137	4.9075	.0029	.0015
		138	4.9124	.0031	.0020
		139	4.9071	.0028	.0013
		140	4.9095	.0035	.0025
		141	4.9052	.0028	.0013
		142	4.9118	.0024	
		143	4.9231	.0024	.0005
		144	4.9409	.0029	.0003
		145	4.9536	.0054	.0005
		146	4.9686	.0027	.0004
		148	4.9986	.0019	.0004
		150	5.0415	.0021	.0005
60	Nd	138	4.9528	.0063	.0011
		139	4.9480	.0063	.0011
		140	4.9491	.0063	.0011
		141	4.9396	.0065	.0018
		142	4.9438	.0063	.0009
		143	4.9396	.0063	.0011
		144	4.9445	.0062	
		145	4.9584	.0063	.0007
		146	4.9746	.0065	.0010
		147	4.9839	.0010	
		148	5.0009	.0016	
		149	5.0108	.0010	
		150	5.0400	.0011	
		151	5.0544	.0093	
		152	5.0842	.0055	
62	Sm	153	5.0940	.0084	
		154	5.1112	.0058	
		138	4.9850	.0175	.0057
		139	4.9792	.0167	.0033
		140	4.9716	.0163	.0012
		141	4.9718	.0162	.0009
		142	4.9628	.0163	.0010
		143	4.9656	.0162	.0005
		144	4.9632	.0162	.0006
		145	4.9682	.0162	—
		146	4.9807	.0164	.0009
		147	4.9954	.0170	.0017

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
63	Eu	148	5.0059	.0176	.0024
		149	5.0215	.0190	.0033
		150	5.0308	.0199	.0039
		151	5.0534	.0041	
		152	5.1075	.0302	.0080
		153	5.1127	.0037	
		154	5.1213	.0317	.0063
		155	5.1200	.0314	.0060
		156	5.1236	.0320	.0063
		157	5.1348	.0146	<u>.0006</u>
		158	5.1408	.0155	<u>.0006</u>
		159	5.1493	.0169	<u>.0007</u>
		64	4.9760	.0134	
		146	5.0819	.0030	.0001
64	Gd	154	5.1253	.0017	
		155	5.1346	.0016	.00003
		156	5.1458	.0014	.0001
		157	5.1492	.0014	.0001
		158	5.1617	.0018	.0001
		160	5.1776	.0020	.0001
		65	4.9211	.1508	.0033
		147	4.9299	.1507	.0030
		148	4.9429	.1506	.0027
		149	4.9429	.1506	.0026
		150	4.9502	.1505	.0023
		151	4.9633	.1504	.0021
		152	4.9691	.1504	.0019
		153	4.9950	.1502	.0016
66	Dy	154	5.0336	.1501	.0019
		155	5.0391	.1500	.0010
		156	5.0487	.1500	.0009
		159	5.0600	.1500	
		146	5.0522	.2030	.0002
		148	5.0538	.2030	—
		149	5.0642	.2035	.0012
		150	5.0772	.2057	.0024
		151	5.0860	.2081	.0034
		152	5.1000	.2133	.0049
		153	5.1079	.2171	.0058
		154	5.1272	.2283	.0078
		155	5.1475	.2428	.0097
67	Ho	156	5.1630	.2556	.0117
		157	5.1712	.2628	.0126
		158	5.1812	.2720	.0136
		159	5.1820	.2728	.0136
		160	5.1938	.2843	.0146
		161	5.1965	.0061	
		162	5.2068	.0027	
		163	5.2091	.0025	
		164	5.2207	.0024	
		151	5.0454	.0349	.0011
		152	5.0660	.0339	.0009
		153	5.0791	.0334	.0009
		154	5.0893	.0329	.0006
68	Er	155	5.1104	.0322	.0005
		156	5.1145	.0322	.0006
		157	5.1549	.0312	.0003
		158	5.1584	.0312	.0004
		159	5.1684	.0310	.0002
		160	5.1672	.0310	.0003
		161	5.1791	.0309	.0002
		162	5.1823	.0309	.0007
		163	5.1909	.0308	.0006
		165	5.2022	.0308	
		150	5.0388	.0287	—

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
69	Tm	152	5.0707	.0291	.0024
		154	5.1016	.0303	.0048
		156	5.1344	.0322	.0074
		158	5.1707	.0353	.0106
		160	5.2019	.0380	.0126
		162	5.2242	.0042	
		164	5.2375	.0037	
		166	5.2505	.0031	
		167	5.2547	.0031	
		168	5.2673	.0037	
		170	5.2857	.0043	
		156	5.1018	.0134	.0006
		157	5.1146	.0074	.0009
		158	5.1239	.0069	.0007
		159	5.1396	.0060	.0004
		160	5.1507	.0055	.0004
		161	5.1619	.0050	.0003
		162	5.1715	.0048	.0005
		163	5.1851	.0042	.0002
		164	5.1908	.0042	.0006
		165	5.2006	.0038	.0002
		166	5.2047	.0038	.0003
		167	5.2130	.0036	.0003
		168	5.2171	.0036	.0004
		169	5.2256	.0035	
		170	5.2304	.0036	.0005
		171	5.2387	.0037	.0006
		172	5.2408	.0052	.0030
70	Yb	152	5.0303	.0136	.0058
		154	5.0790	.0132	.0056
		156	5.1158	.0130	.0055
		158	5.1427	.0091	.0006
		160	5.1721	.0079	.0004
		161	5.1832	.0075	.0003
		162	5.2005	.0069	.0003
		163	5.2112	.0066	.0002
		164	5.2269	.0063	.0003
		165	5.2364	.0061	.0002
		166	5.2496	.0059	.0001
		167	5.2595	.0059	.00005
		168	5.2678	.0059	—
		170	5.2830	.0058	.0001
		171	5.2891	.0060	.0001
		172	5.2978	.0053	.0002
		173	5.3041	.0046	.0002
		174	5.3115	.0057	.0003
		176	5.3228	.0069	.0003
71	Lu	161	5.2313	.0112	.0006
		162	5.2416	.0102	.0005
		163	5.2582	.0087	.0004
		164	5.2690	.0077	.0004
		165	5.2841	.0064	.0003
		166	5.2981	.0053	.0002
		167	5.3115	.0044	.0002
		168	5.3233	.0038	.0001
		169	5.3294	.0036	.0001
		170	5.3368	.0302	—
		171	5.3439	.0302	.0001
		172	5.3488	.0302	.0001
		173	5.3578	.0303	.0001
		174	5.3635	.0303	.0001
		175	5.3700	.0300	.0002
		176	5.3738	.0304	.0002
		177	5.3812	.0305	.0002

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
72	Hf	178	5.3855	.0306	.0002
		179	5.3914	.0307	.0003
		170	5.2876	.0056	.0007
		172	5.3047	.0043	.0005
		173	5.3123	.0039	.0004
		174	5.3185	.0035	.0003
		175	5.3175	.0037	.0011
		176	5.3305	.0037	.0002
		177	5.3331	.0038	.0001
		178	5.3356	.0031	
		179	5.3358	.0024	.0001
		180	5.3422	.0024	.0002
		182	5.3481	.0037	.0011
		73	5.3507	.0034	
		74	5.3493	.0023	.0008
		182	5.3566	.0017	
		183	5.3300	.1500	.0005
		184	5.3670	.0017	.0008
		186	5.3759	.0019	.0007
75	Re	185	5.3286	.0126	
		187	5.3386	.0127	.0009
		76	5.3820	.0023	.0010
		186	5.3908	.0016	
		187	5.3934	.0017	.0005
		188	5.3994	.0011	.0009
		189	5.3600	.1500	.0010
		190	5.4061	.0009	
		192	5.4127	.0011	
		182	5.3809	.1061	.0006
		183	5.3857	.1061	.0005
		184	5.3881	.1061	.0005
		185	5.3899	.1061	.0005
		186	5.3943	.1061	.0005
		187	5.3881	.1061	.0005
		188	5.3890	.1061	.0005
		189	5.3938	.1061	.0005
		191	5.3981	.1061	
77	Ir	193	5.4019	.1061	.0005
		178	5.3721	.0070	.0015
		179	5.3915	.0055	.0020
		180	5.3890	.0051	.0010
		181	5.3998	.0044	.0014
		182	5.3971	.0043	.0009
		183	5.4033	.0037	.0007
		184	5.4028	.0037	.0006
		185	5.4155	.0029	.0006
		186	5.4046	.0039	.0011
		187	5.4074	.0041	.0019
		188	5.4059	.0035	.0007
		189	5.4068	.0037	.0012
		190	5.4117	.0032	.0007
		191	5.4110	.0032	.0007
		192	5.4181	.0029	.0009
		193	5.4201	.0027	.0006
		194	5.4247	.0025	
		195	5.4278	.0026	.0004
		196	5.4315	.0032	.0004
78	Pt	198	5.4403	.0063	.0007
		184	5.4298	.0041	.0011
		185	5.4288	.0040	.0008
		186	5.4345	.0038	.0007
		187	5.4002	.0058	.0008
		188	5.4037	.0055	.0008
		79	5.4277	.0062	.0012
		183	5.3877	.0062	.0012
		184	5.4298	.0041	.0011
		185	5.4288	.0040	.0008
80	Au	186	5.4345	.0038	.0007
		187	5.4002	.0058	.0008
		188	5.4037	.0055	.0008
		189	5.4277	.0062	.0012
		190	5.4298	.0041	.0011
		191	5.4288	.0040	.0008
		192	5.4345	.0038	.0007
		193	5.4002	.0058	.0008

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
80	Hg	189	5.4072	.0051	.0006
		190	5.4095	.0049	.0006
		191	5.4134	.0046	.0005
		192	5.4166	.0044	.0005
		193	5.4213	.0042	.0004
		194	5.4239	.0040	.0002
		195	5.4284	.0040	.0006
		196	5.4318	.0038	.0004
		197	5.4358	.0037	
		198	5.4386	.0038	.0002
		199	5.4440	.0039	.0001
		181	5.4373	.0032	.0003
		182	5.3844	.0053	.0003
		183	5.4415	.0031	.0003
		184	5.3946	.0047	.0003
		185	5.4406	.0031	.0003
		186	5.4014	.0044	.0003
		187	5.4046	.0043	.0003
81	Tl	188	5.4083	.0041	.0003
		189	5.4098	.0040	.0003
		190	5.4157	.0038	.0003
		191	5.4171	.0037	.0003
		192	5.4233	.0035	.0003
		193	5.4239	.0035	.0003
		194	5.4311	.0033	.0003
		195	5.4347	.0032	.0003
		196	5.4388	.0032	.0003
		197	5.4415	.0031	.0003
		198	5.4466	.0031	
		199	5.4484	.0031	.0003
		200	5.4549	.0023	.0003
		201	5.4583	.0025	.0003
		202	5.4633	.0015	.0003
		203	5.4687	.0035	.0003
		204	5.4742	.0013	.0003
		205	5.4788	.0031	.0003
		206	5.4851	.0031	.0003
82	Pb	188	5.3985	.0092	.0015
		189	5.4235	.0063	.0007
		190	5.4088	.0081	.0013
		191	5.4138	.0070	.0003
		192	5.4161	.0073	.0012
		193	5.4302	.0058	.0008
		194	5.4233	.0065	.0010
		195	5.4303	.0055	.0003
		196	5.4304	.0058	.0009
		197	5.4370	.0048	.0002
		198	5.4376	.0048	.0001
		199	5.4466	.0040	.0001
83	Po	200	5.4477	.0039	.0001
		201	5.4564	.0034	.0003
		202	5.4587	.0033	.0003
		203	5.4664	.0026	.0002
		205	5.4763	.0026	
		207	5.4862	.0028	.0002
		208	5.4963	.0031	.0006
		190	5.4210	.0026	.0011
		191	5.4217	.0026	.0011
		192	5.4287	.0025	.0011
		193	5.4298	.0022	.0007
		194	5.4359	.0022	.0009
84	Bi	196	5.442	.0105	.0014
		197	5.4420	.0105	.0014
		198	5.4500	.0085	.0012
		199	5.4500	.0085	.0012
		200	5.4590	.0075	.0010
		201	5.4610	.0075	.0009
		202	5.4690	.0055	.0007
		203	5.4710	.0055	.0007
		204	5.4794	.0008	.0005
		205	5.4820	.0035	.0005
		206	5.4897	.0007	.0003
		207	5.4942	.0013	.0002
85	Rn	208	5.5010	.0009	
		209	5.5110	.0025	.0002
		210	5.5230	.0035	.0005
		211	5.5330	.0055	.0007
		212	5.5450	.0075	.0010
		214	5.5650	.0105	.0014
		209	5.5211	.0026	
		200	5.4861	.0133	.0007
		202	5.4936	.0131	.0003
		204	5.5025	.0130	.0002
		205	5.5044	.0130	.0006
		206	5.5123	.0129	.0001
86	Fr	207	5.5147	.0129	.0005
		208	5.5222	.0129	
		209	5.5264	.0129	.0004
		210	5.5336	.0129	.0003
		202	5.5150	.0136	.0001
		204	5.5197	.0134	.00009
		205	5.5198	.0134	.00009
		206	5.5270	.0132	.00007
		207	5.5282	.0132	.00007
		208	5.5354	.0131	.00005
		209	5.5373	.0131	.00004
		210	5.5442	.0130	.00002
87	Ra	211	5.5479	.0130	.00002
		212	5.5545	.0130	
		218	5.6172	.0144	.0001
		219	5.6280	.0149	.0001
		220	5.6363	.0153	.0001
		221	5.6467	.0159	.0002
		222	5.6549	.0164	.0002
		207	5.5349	.0130	.00005
		208	5.5358	.0130	.00005
		209	5.5428	.0130	.00003
		210	5.5448	.0130	.00002
		211	5.5511	.0130	.00001
88	Ra	212	5.5545	.0130	
		213	5.5606	.0130	.00002
		220	5.6320	.0130	.0001
		221	5.6422	.0131	.0002
		222	5.6523	.0131	.0002
		223	5.6584	.0131	.0002
		224	5.6695	.0132	.0002
		225	5.6747	.0132	.0003
		226	5.6825	.0132	.0003
		227	5.6972	.0133	.0003
		228	5.7036	.0133	.0003
		208	5.5475	.0138	.0024
89	Ra	209	5.5478	.0137	.0022
		210	5.5542	.0134	.0017
		211	5.5554	.0133	.0015
		212	5.5616	.0131	.0009
		213	5.5646	.0130	.0006
		214	5.5705	.0130	
		220	5.6311	.0178	.0062

Table 1 (continued)

Z	El	A	R (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
199		5.4500	.0085	.0012	
200		5.4590	.0075	.0010	
201		5.4610	.0075	.0009	
202		5.4690	.0055	.0007	
203		5.4710	.0055	.0007	
204		5.4794	.0008	.0005	
205		5.4820	.0035	.0005	
206		5.4897	.0007	.0003	
207		5.4942	.0013	.0002	
208		5.5010	.0009		
209		5.5110	.0025	.0002	
210		5.5230	.0035	.0005	
211		5.5330	.0055	.0007	
212		5.5450	.0075	.0010	
213		5.5550	.0105	.0014	
214		5.5650	.0105	.0014	
215		5.5750	.0130	.0022	
216		5.5850	.0130	.0022	
217		5.5950	.0130	.0022	
218		5.6050	.0130	.0022	
219		5.6150	.0130	.0022	
220		5.6250	.0130	.0022	
221		5.6350	.0130	.0022	
222		5.6450	.0130	.0022	
223		5.6550	.0130	.0022	
224		5.6650	.0132	.0022	
225		5.6750	.0132	.0022	
226		5.6850	.0132	.0022	
227		5.6950	.0133	.0023	
228		5.7050	.0133	.0023	
229		5.7150	.0133	.0023	
230		5.7250	.0133	.0023	
231		5.7350	.0133	.0023	
232		5.7450	.0133	.0023	
233		5.7550	.0133	.0023	
234		5.7650	.0133	.0023	
235		5.7750	.0133	.0023	
236		5.7850	.0133	.0023	
237		5.7950	.0133	.0023	
238		5.8050	.0133	.0023	
239		5.8150	.0133	.0023	
240		5.8250	.0133	.0023	
241		5.8350	.0133	.0023	
242		5.8450	.0133	.0023	
243		5.8550	.0133	.0023	
244		5.8650	.0133	.0023	
245		5.8750	.0133	.0023	
246		5.8850	.0133	.0023	
247		5.8950	.0133	.0023	
248		5.9050	.0133	.0023	
249		5.9150	.0133	.0023	
250		5.9250	.0133	.0023	
251		5.9350	.0133	.0023	
252		5.9450	.0133	.0023	
253		5.9550	.0133	.0023	
254		5.9650	.0133	.0023	
255		5.9750	.0133	.0023	
256		5.9850	.0133	.0023	
257		5.9950	.0133	.0023	
258		6.0050	.0133	.0023	
259		6.0150	.0133	.0023	
260		6.0250	.0133	.0023	
261		6.0			

Table 1 (*continued*)

<i>Z</i>	El	<i>A</i>	<i>R</i> (fm)	$\Delta_{\text{tot}}R$ (fm)	$\Delta_{\text{rel}}R$ (fm)
90	Th	221	5.6423	.0195	.0073
		222	5.6502	.0207	.0081
		223	5.6602	.0222	.0091
		224	5.6676	.0234	.0098
		225	5.6781	.0252	.0109
		226	5.6841	.0263	.0115
		227	5.6911	.0276	.0123
		228	5.7002	.0292	.0132
		229	5.7088	.0308	.0140
		230	5.7186	.0325	.0150
		232	5.7351	.0356	.0167
		227	5.6654	.0516	.0061
		228	5.6738	.0512	.0049
		229	5.6807	.0509	.0040
		230	5.6920	.0506	.0025
92	U	232	5.7100	.0504	
		233	5.8138	.0074	.0043
		234	5.8289	.0062	.0033
		235	5.8287	.0073	.0027
		236	5.8366	.0074	.0016
		238	5.8507	.0072	
94	Pu	238	5.8248	.0378	.0012
		239	5.8311	.0378	
		240	5.8407	.0379	.0016
		241	5.8451	.0379	.0019
		242	5.8523	.0380	.0024
		244	5.8643	.0382	.0032
95	Am	241	5.8929	.0035	
		243	5.9047	.0035	
96	Cm	242	5.7851	.0149	.0049
		244	5.7995	.0134	
		245	5.8040	.0135	.0010
		246	5.8127	.0138	.0020
		248	5.8252	.0149	.0040

Table 2

Parameters of radius formulae for nuclei near the stability line. See page 194 for Explanation of Tables

Model	Equation	Parameters	St. Dev. (fm)	χ^2/n'
Liquid drop	(6)	$r_{LD} = 0.9542(13) \text{ fm}$	0.106	2894
Empirical exponent	(7)	$r_e = 1.153(7) \text{ fm}$ $e = 0.2938(12)$	0.05	669
Finite surface	(8)	$r_0 = 0.9071(13) \text{ fm}$ $r_1 = 1.105(25) \text{ fm}$ [$r_2 = -0.548(34) \text{ fm}$]	0.04	467
Finite surface + P	(15)	$r_{0,P} = 0.8966(20) \text{ fm}$ $r_{1,P} = 1.128(35) \text{ fm}$ [$r_{2,P} = -0.58(05) \text{ fm}$] $a = 0.0809(19) \text{ fm}^2$	0.023	167
Finite surface + P (light nuclei)	(15)	$r_{0,P} = 0.982(10) \text{ fm}$ $r_{1,P} = 0.32(10) \text{ fm}$ [$r_{2,P} = +0.55(14) \text{ fm}$] $a = 3.93(42) \text{ fm}^2$	0.034	93

Table 3

Empirical parameters characterizing the radius surface $R(N, Z)$. See page 194 for Explanation of Tables

Equation	Parameter	Region	From experiment	St. Dev. (fm)	χ^2/n'	With constraint
(9)	k_Z	All nuclids	0.149(15)	0.036	64	0.156(14)
		Proton-rich	0.131(25)	0.027	27	0.128(23)
		Neutron-rich	0.219(30)	0.025	35	0.240(27)
(10)	k_N	All nuclids	0.484(15)	0.027	29	0.478(14)
		Proton-rich	0.482(25)	0.027	23	0.485(23)
		Neutron-rich	0.484(30)	0.017	20	0.463(27)
(12)	f	All nuclids	-0.148(15)	0.032	38	-0.161(9)
		Proton-rich	-0.185(25)	0.027	17	-0.179(14)
		Neutron-rich	-0.070(30)	0.019	16	-0.112(17)
(13)	$\Delta Z/\Delta N$	All nuclids	-0.33(4)	0.035	34	-0.33(4)
		Proton-rich	-0.25(6)	0.029	18	-0.25(5)
		Neutron-rich	-0.67(10)	0.027	19	-0.62(8)

Table 4

Annotated references for the Introduction and for the Tables. See page 194 for Explanation of Tables

References for the Introduction*Compilations*

- An99 I.Angeli: *Table of Nuclear Root Mean Square Charge Radii*, $e^- + \mu^-$, $e^- + \mu^- + OIS$, INDC(HUN)-033, September 1999 (IAEA Nuclear Data Section, Vienna)
Web: <http://www-nds.iaea.or.at/indc-sel.html>.
- Au87 P.Aufmuth, et al.: *At. Data Nucl. Data Tables*, **37** (1987) 455 *OIS*
- Bo74 F.Bohm, and P.L.Lee: *At. Data Nucl. Data Tables*, **14** (1974) 605 K_zIS
- En74 R.Engfer, et al.: *At. Data Nucl. Data Tables*, **14** (1974) 509 μ^-
- Fr95 G.Fricke, et al.: *At. Data Nucl. Data Tables*, **60** (1995) 177, Table V Many; compilation.
- He74 K.Heilig, and A.Steudel: *At. Data Nucl. Data Tables*, **14** (1974) 613 *OIS*
- Ho67 R.Hofstadter, and H.R.Collard: *Landolt-Börnstein, New series, Group I*: e^- , μ^- , K_zIS , *OIS*
Nuclear Physics and Technology, vol. 2, Nuclear Radii, ed. H.Schopper, Springer-Verlag, Berlin (1967)
- Ja74 C.W.deJager, et al.: *At. Data Nucl. Data Tables*, **14** (1974) 479 e^-
- Na94 E.G.Nadjakov, et al.: *At. Data Nucl. Data Tables*, **56** (1994) 133 $e^- + \mu^- + OIS$
- Ot89 E.W.Otten: in: *Treatise in Heavy-Ion Physics*, Vol. 8 (1989) 604 *OIS*
- Vr87 H.deVries, et al.: *At. Data Nucl. Data Tables*, **36** (1987) 495 e^-

Other papers

- Ah85 S.A.Ahmad, et al.: *Z. Physik*, **A321** (1985) 35 Eu
- Ah88 S.A.Ahmad, et al.: *Nucl. Phys.*, **A483** (1988) 244 Ra
- An77 I.Angeli, and M.Csatlós: *Nucl. Phys.*, **A288** (1977) 480 Isotopic dependence $R_Z(N)$
- An78 I.Angeli, and M.Csatlós: *ATOMKI Közlemények*, **20** (1978) 1 Isotonic, isobaric dep.
- An91 I.Angeli: *J.Phys. G: Nucl. Part. Phys.*, **17** (1991) 439 Fine structure in $R(A)$
- An91a I.Angeli: *Acta Phys. Hung.*, **69** (1991) 233 Compilation
- An92 I.Angeli: *AMCO-9, 9th Conf. on Atomic Masses and Fundamental Constants*; July 19–24, 1992, Bernkastel-Kues Mass number dependence $R(A_0)$
- An00 I.Angeli: *Acta Phys. Hung. New Series: Heavy Ion Physics*, **13** (2001) 149 I -dependence
- An01 I.Angeli: *Hyperfine Interactions*, **136** (2001) 17 K_zIS : C_1
- An02 I.Angeli: *Acta Phys. Hung. New Series: Heavy Ion Physics*, **15** (2002) 87 μ^- : Barrett mom.
- An03 I.Angeli: *Acta Phys. Hung. New Series: Heavy Ion Physics*, **17** (2003) 3 OIS: eval.
- Ba70 R.C.Barrett: *Physics Letters*, **B33** (1970) 388 Theory
- Bl87 S.A.Blundell, et al: *J. Phys.*, **B20** (1987) 3663 K_zIS , theory
- Ca87 R.F.Casten, et al: *Phys. Rev. Lett.*, **58** (1987) 658 P-factor
- El61 L.R.B.Elton: *Nuclear Sizes* (Oxford University Press, 1961) Formula $R(A)$
- Ga30 G.Gamow: *Proc. Roy. Soc. London*, **A216** (1930) 632 Formula $R(A)$
- He87 K.Heilig: *Hyperfine Interactions*, **38** (1987) 803 Evaluation
- He89 J.Herberz: *Ph.D. thesis, Univ. Mainz, KPH 6/89* (1989) O, F, Na, Ne, Mg, Al, Si
- Hu98 A.Huber, et al.: *Phys. Rev. Letters*, **80** (1998) 468 D
- Kr99 A.Krasznahorkay, et al.: *Phys. Rev. Letters*, **82** (1999) 3216 Neutron skin
- Me00 K.Melnikov, and T. van Ritbergen: *Phys. Rev. Lett.*, **84** (2002) 1673 H
- My83 W.D.Myers, and K.H.Schmidt: *Nucl. Phys.*, **A410** (1983) 61 Formulae $R(N, Z)$
- Sc69 J.P.Schiffer: *Physics Letters*, **29B** (1969) 399 Isotopic dependence $R_Z(N)$
- Se69 E.C.Seltzer: *Phys. Rev.*, **188** (1969) 1916 Theory: $C_{1,2,3}$ coeffs.
- Si98 I.Sick, and D.Trautmann: *Nucl. Phys.*, **A637** (1998) 559 D
- Si03 I.Sick: *Physics Letters*, **B576** (2003) 62 H
- St66 D.N.Stacey: *Rep. Prog. Phys.*, **29** (1966) 171 Fine structure in $R_Z(N)$
- To85 G.Torbohm, et al: *Phys. Rev.*, **A31** (1985) 2038 K_zIS , theory
- Un75 M.Uno, and M.Yamada: *Progr. Theor. Phys.*, **53** (1975) 987 Fine structure in E
- Un81 M.Uno, and M.Yamada: *Progr. Theor. Phys.*, **65** (1981) 1322 Fine structure in E
- We85 E.Wesolowski: *J. Phys. G: Nuc. Part. Phys.*, **11** (1985) 909 Formulae $R(NZ)$
- Ze81 N.Zeldes: *Proc. 4th Int. Conf. on Nuclei Far From Stability*, Helsingør, Denmark, Eds. P.G.Hansen, and O.B.Nielsen, **Vol. I** (Geneva, CERN, 1981) p.93.....

References for the Tables*Differences between radii of neighboring nuclei (not isotopes) from electron scattering and muonic atom X-rays*

- Fr92 G.Fricke, et al.: *Phys. Rev.*, **C45** (1992) 80, Table III O, F, Ne, Na, Mg, Al, Si
- Fr95 G.Fricke, et al.: *At. Data Nucl. Data Tables*, **60** (1995) 177, Table VII Many; compilation
- He89 J.Herberz: *Ph.D. thesis, Univ. Mainz, KPH 6/89* (1989) O, F, Na, Ne, Mg, Al, Si
- Vr87 H.de Vries, et al.: *At. Data Nucl. Data Tables*, **36** (1987) 495, Table III Many; compilation.
- Wo80 H.D.Wohlfahrt, et al.: *Phys. Rev.*, **C22** (1980) 264 Ti, Cu Zn
- Wo81 H.D.Wohlfahrt, et al.: *Phys. Rev.*, **C23** (1981) 533, Table VI K,Ca,Sc,Ti,V,Cr,Mn,Fe

Differences between radii of isotopes, from electron scattering

- Ja74 C.W.de Jager, et al.: *At. Data Nucl. Data Tables*, **14** (1974) 479, Table II Many; compilation.
- Ro76 H.Rothhaas, *Ph.D. Thesis, Univ. Mainz* (1976). **KPH 18/76** Zr
- Vr87 H.de Vries, et al.: *At. Data Nucl. Data Tables*, **36** (1987) 495, Table II Many; compilation.

Table 4 (continued)

Differences between radii of isotopes, from muonic atom X-rays		
Ba80	G.Backenstoss, et al.: <i>Physics Letters</i> , 95B (1980) 212.....	O
En74	R.Engfer, et al.: <i>At. Data Nucl. Data Tables</i> , 14 (1974) 509, Table IV	Many; compilation.
Fr92	G.Fricke, et al.: <i>Phys. Rev.</i> C45 (1992) 80, Table III.....	O, Ne, Mg, Al, Si
Fr95	G.Fricke, et al.: <i>At. Data Nucl. Data Tables</i> , 60 (1995) 177, Table V	Many; compilation.
He89	J.Herberz: <i>Ph.D. thesis, Univ. Mainz, KPH 6/89</i> (1989).....	O, F, Na, Ne, Mg, Al, Si
Ho81	M.V.Hoehn, et al.: <i>Phys. Rev.</i> C24 (1981) 1667	Os
La83	D.B.Laubacher, et al.: <i>Phys. Rev.</i> C27 (1983) 1772	Gd
Ma89	P.Mazanek: <i>Dipl. Th., Inst. f. Kernph. PKH 11/89</i> , U. Mainz 1989.....	Zr, Mo
Ma92a	P.Mazanek, <i>Ph.D. Th. Inst. f. Kernph. PKH 5/92</i> , U. Mainz 1992	Pb
Po79	R.J.Powers, et al.: <i>Nucl. Phys.</i> A316 (1979) 295, Table 18.....	Sm
Sc80	L.Schellenberg, et al.: <i>Nucl. Phys.</i> A333 (1980) 333	Mo
Sc82	L.A.Schaller, et al.: <i>Nucl. Phys.</i> A379 (1982) 523	C
Sc85	L.A.Schaller, et al.: <i>Phys. Rev.</i> C31 (1985) 1007	S
Sh82	E.B.Shera, et al.: <i>Physics Letters</i> , 112B (1982) 124	Ba
Ta84	Y.Tanaka, et al.: <i>Phys. Rev.</i> C29 (1984) 1897	Eu
Ta84a	Y.Tanaka, et al.: <i>Phys. Rev.</i> C30 (1984) 350	Hf
Wo80	H.D.Wohlfahrt, et al.: <i>Phys. Rev.</i> C22 (1980) 264	Ti, Cu Zn
Wo81	H.D.Wohlfahrt, et al.: <i>Phys. Rev.</i> C23 (1981) 533, Table VI.....	Ca, Ti, Cr
Differences between radii of isotopes, from atomic K_{α} isotope shifts		
Bh68	S.K.Bhattacherjee, et al.: <i>Phys. Rev. Letters</i> , 20 (1968) 1295.....	Nd
Bh69	S.K.Bhattacherjee, et al.: <i>Phys. Rev.</i> , 188 (1969) 1919	Gd, Dy, Er, Hf + prev.: Sn, Nd, Sm, W, Hg, Pb, U
Bl87	S.A.Blundell, et al.: <i>J. Phys.</i> , B20 (1987) 3663	Theory: S_4, S_6 calc.
Bo81	G.L.Borchert et al: 4 th <i>I. C. Nucl. far from Stab.</i> L.O.Skolen, 1981, I , p.56	Pb
Bo83	G.L.Borchert, et al.: <i>Nuovo Cimento</i> , A73 (1983) 273	Pb
Br65	R.T.Brockmeier, et al.: <i>Phys. Rev. Lett.</i> , 15 (1965) 132	U
Ch67	R.B.Chesler, et al.: <i>Phys. Rev. Letters</i> , 18 (1967) 953	Sn, Sm, W
Ch68	R.B.Chesler, and F.Boehm: <i>Phys. Rev.</i> 166 (1968) 1206	Sn,Nd,Sm,Gd,W,Hg,Pb
Ei70	C.W.E. van Eijk, and F.Schutte: <i>Nucl. Phys.</i> A151 (1970) 459	Dy
Ei70a	C.W.E. van Eijk, and M.J.C.Visscher: <i>Phys. Lett.</i> , 34B (1970) 349.....	Ce
Ei79	C.W.E.Eijk, et al.: <i>Journ. Phys.</i> G5 (1979) 315	Cd
El96	S.R.Elliott, et al.: <i>Phys. Rev. Lett.</i> , 76 (1996) 1031	U, see El96 er
El96er	S.R.Elliott, et al.: <i>Phys. Rev. Lett.</i> , 77 (1996) 4278 (erratum)	U corrected.
Le73	P.L.Lee, and F.Boehm: <i>Phys. Rev.</i> C8 (1973) 819	Nd, Sm, Dy, Yb, Pb
Le78	P.L.Lee, F.Boehm, and A.A.Hahn: <i>Phys. Rev.</i> C17 (1978) 1859	Hg
Ry72	A.S.Rylnikov, et al.: <i>Journ. Exp. Theor. Phys.</i> 63 (1972) 53	Sb, Eu
Su65	O.I.Sumbaev, and A.F.Mezentsev: <i>Journ. Exp. Theor. Phys.</i> 49 (1965)459	Mo
Su67	O.I.Sumbaev, et al.: <i>Yadernaya Fizika</i> , 5 (1967) 544	Nd, Sm
Su68	O.I.Sumbaev, "Nuclear Structure", IAEA Vienna, 1968, p.527	Mo,Ba,Nd,Sm
Su69	O.I.Sumbaev: <i>Int. C. Prop. Nucl. St. Montreal</i> , Aug. 25-30 1969. Contr. 2.67	Te
Su69a	O.I.Sumbaev, et al.: <i>Yadernaya Fizika</i> , 9 (1969) 906	Ba
To85	G.Torbohm, et al.: <i>Phys. Rev.</i> , A31 (1985) 2038	Theory: C_i/C_1 calc.
Special case: H-D isotope shift		
Hu98	A.Huber, et al.: <i>Phys. Rev. Letters</i> , 80 (1998) 468	H-D Isotope Shift
Pa94	K.Pachucki, et al.: <i>Phys. Rev.</i> A49 (1994) 2255	H-D IS theory
Sc93	F.Schmidt-Kaler, et al.: <i>Phys. Rev. Letters</i> , 70 (1993) 2261.....	Re-anal in Pa94, We95
We92	M.Weitz: <i>Ph.D. Thesis, Max-Planck-Institut für Quantenoptik</i> (1992)	Re-anal in Pa94, We95
We95	M.Weitz, et al.: <i>Phys. Rev.</i> A52 (1995) 2664	H-D Lamb-shift, IS.
Differences between isotopes from optical isotope shifts		
Ah85	S.A.Ahmad, et al.: <i>Z. Physik</i> , A321 (1985) 35	Eu
Ah88	S.A.Ahmad, et al.: <i>Nucl. Phys.</i> , A483 (1988) 244	Ra
Al79	E.Alvarez, et al.: <i>Physica Scripta</i> , 20 (1979) 141	Xe
Al83	G.D.Alhazov, et al.: <i>Zhurn.Exp.Teor. Fiz. Letters</i> , 37 (1983) 231	Eu
Al85	G.D.Alhazov, et al.: <i>Izv. Ak. Nauk SSSR, Ser. Fiz.</i> , 49 (1985) 24	Sm, Eu
Al85a	G.D.Alhazov, et al.: <i>Tez. Dok. XXXV. Sov. Leningrad</i> (1985)	Tm
Al86a	G.D.Alhazov, et al.: <i>Yadernaya Fizika</i> , 44 (1986) 1134	Sm, Eu
Al87	G.D.Alhazov, et al.: <i>Tez. Dokl. XXXVII. Soveshch.</i> (1987) 96	Nd, Sm
Al88	G.D.Alhazov, et al.: <i>Nucl. Phys.</i> , A477 (1988) 37	Tm
Al88a	G.D.Alhazov, et al.: <i>Pisma v Zs.E.T.F.</i> , 48 (1988) 373	Gd
Al89	G.D.Alhazov, et al.: <i>Nucl. Phys.</i> , A504 (1989) 549	Ho
Al90	G.D.Alhazov, et al.: <i>Z. Phys.</i> , A337 (1990) 367	Tb
Al90a	G.D.Alhazov, et al.: <i>Z. Phys.</i> , A337 (1990) 257	Eu
An82	A.Andl, et al.: <i>Phys. Rev.</i> , C26 (1982) 2194	Ca

Table 4 (continued)

An86	M.Anselment, et al.: <i>Phys. Rev.</i> , C34 (1986) 1052	Sn
An86b	M.Anselment: <i>Nucl. Phys.</i> A451 (1986)471 [Corrected in: KFK 4159 p.63.]	Pb
An87	M.Anselment, et al.: <i>Z. Phys.</i> , A326 (1987) 493	Sr
An92	A.Anastassov, et al.: <i>Hyperfine Interactions</i> , 74 (1992) 31	Hf, U
An94	A.Yu.Anastassov, et al.: <i>Zhurn.Exp.Teor. Fiz.</i> 105 (1994) 250	Hf
An94a	A.Anastassov, et al.: <i>Z. Phys.</i> , D30 (1994) 275	Ti
Au78	P.Aufmuth, et al.: <i>Z. Physik</i> , A285 (1978) 357	Mo
Au83	P.Aufmuth, and M.Haunert: <i>Physica</i> , 123C (1983) 109	Zr
Ba76	P.E.G.Baird: <i>Proc. Roy. Soc. London</i> , A351 (1976) 267	Pd
Ba79	P.E.G.Baird, et al.: <i>Proc. Roy. Soc. London</i> , A365 (1979) 567	Ba
Ba83	P.E.G.Baird, et al.: <i>J. Phys.</i> , B16 (1983) 2485	Sn
Ba85	J.Bauche, et al.: <i>Z. Physik</i> , A320 (1985) 157	Cd; eval. of Br76
Ba98	A.E.Barzakh, et al.: <i>Eur. Phys. J.</i> , A_1 (1998) 3	Yb
Ba00	A.E.Barzakh, et al.: <i>Phys. Rev.</i> , C61 (2000) 034304	Tm
Be79	K.Bekk, et al.: <i>Z. Physik</i> , A291 (1979) 219	Ba
Be80	E.Bergmann, et al.: <i>Z. Physik</i> , A294 (1980) 319	Ca
Be84	D.Bender, et al.: <i>Z. Physik</i> , A318 (1984) 291	Sr
Be85	A.Bernard, et al.: <i>Z. Physik</i> , A322 (1985) 1	Er
Bl87	S.A.Blundell, et al.: <i>J. Phys.</i> , B20 (1987) 3663	Theory: S ₄ , S ₆ calc.
Bo76	J.Bonn, et al.: <i>Z. Physik</i> , A276 (1976) 203	Hg
Bo79	J.Bonn, et al.: <i>Z. Physik</i> , A289 (1979) 227	Cs
Bo81	G.Borghs, et al.: <i>Z. Physik</i> , A299 (1981) 11	Xe
Bo84	G.Bollen, et al.: <i>Proc. AMCO-7, Darmstadt</i> (1984) p. 347	Au
Bo87a	S.K.Borisov, et al.: <i>Zhurn.Exp.Teor. Fiz.</i> 93 (1987) 1545	Nd, Sm, Gd
Br58	G.Breit: <i>Rev. Mod. Phys.</i> , 30 (1958) 507	Basic OIS
Br58a	P.Brix: <i>Rev. Mod. Phys.</i> , 30 (1958) 517	Basic OIS
Br76	M.S.W.M.Brimicombe, et al.: <i>Proc. R. Soc. Lond.</i> , A352 (1976) 141	Cd; eval in Ba85
Br78	H.-W.Brandt, et al.: <i>Z. Physik</i> , A288 (1978) 241	Ca
Br79	H.-W.Brandt, et al.: <i>Z. Physik</i> , A291 (1979) 97	Sm
Br80	H.Brand, et al.: <i>Z. Physik</i> , A296 (1980) 281	Sm
Br81	H.Brand, et al.: <i>Z. Physik</i> , A302 (1981) 291	Eu
Bu85	F.Buchinger, et al.: <i>Phys. Rev.</i> , C32 (1985) 2058	Sr
Bu87	F.Buchinger, et al.: <i>Nucl. Phys.</i> , A462 (1987) 305	Cd
Bu90	F.Buchinger, et al.: <i>Phys. Rev.</i> , C41 (1990)	Sr
Bu03	B.A.Bushaw, et al.: <i>Phys. Rev. Letters</i> , 91 (2003) 043004	Li
Ca95	P.Campbell, et al.: <i>Physics Letters</i> , B346 (1995) 21	Bi
Ca02	P.Campbell, et al.: <i>Phys. Rev. Letters</i> , 89 (2002) 082501	Zr
Cl79	D.L.Clark, et al.: <i>Phys. Rev.</i> , A20 (1979) 239	Yb
Cl82	D.L.Clark, and D.W.Greenlees: <i>Phys. Rev.</i> , C26 (1982) 1636	Dy
Co85	A.Coc, et al.: <i>Physics Letters</i> , B163 (1985) 66	Fr
Co87	A.Coc, et al.: <i>Nucl. Phys.</i> , A468 (1987) 1	Cs, Fr
Di87	U.Dinger, et al.: <i>Z. Physik</i> , A328 (1987) 253	Pb
Dö84	K.Dörschel, et al.: <i>Z. Physik</i> , A317 (1984) 233	Eu
Du89	H.T.Duong, et al.: <i>Physics Letters</i> , B217 (1989) 401	Pt
Du90	S.B.Dutta, et al.: <i>Phys. Rev.</i> , C42 (1990) 1911	Gd
Du91	S.B.Dutta, et al.: <i>Z. Phys.</i> , A341 (1991) 39	Pb
Ea84	D.A.Eastham, et al.: <i>J. Phys.</i> , G10 (1984) L 271	Sm
Ea84a	D.A.Eastham, et al.: <i>Z. Physik</i> , A318 (1984) 243	Sm
Ea86	D.A.Eastham, et al.: <i>J. Phys.</i> , G12 (1986) L205	Sr
Ea87	D.A.Eastham, et al.: <i>Phys. Rev.</i> , C36 (1987) 1583	Sr
Eb87	J.Eberz, et al.: <i>Z. Physik</i> , A326 (1987) 121	Sn
Eb87a	J.Eberz, et al.: <i>Nucl. Phys.</i> , A464 (1987) 9	In
Fi75	W.Fischer, et al.: <i>Z. Physik</i> , A274 (1975) 79	Ag
Fo02	D.H.Forest, et al.: <i>J. Phys. G:Nucl. Part. Phys.</i> , 28 (2002) L63	Zr
Ga87	Yu.P.Gangrsky, et al.: <i>Tez. Dokl. XXXVII. Soveshch.</i> (1987) 103	Sm, Gd
Ga88a	Yu.P.Gangrsky, et al.: <i>Zhurn.Exp.Teor. Fiz.</i> , 94 (1988) 9	Zr
Ga89c	Yu.P.Gangrsky, et al.: <i>Yadernaya Fizika</i> , 50 (1989) 1217	Ce
Ge79	H.Gerhardt, et al.: <i>Z. Physik</i> , A292 (1979) 7	Kr
Ge81	H.Gerhardt, et al.: <i>Hyperfine Interactions</i> , 9 (1981) 175	Kr, Xe
Ge98	U.Georg, et al.: <i>Eur. Phys. J.</i> , A_3 (1998) 225	Lu
Ge02	R.W.Geithner, CERN-Thesis, 2002-030	Ne
Go85	A.T.Goble, and C.W.P.Palmers: <i>J. Phys.</i> , B18 (1985) 2181	Mo
Gr82	P.Grundevik, et al.: <i>Z. Physik</i> , A306 (1982) 195	Ba
He85	K.Heilig: <i>Hyperfine Interactions</i> , 24 (1985) 349	Many. Review.
He87	K.Heilig: <i>Hyperfine Interactions</i> , 38 (1987) 803	Evaluation
Hi92	Th.Hilberath, et al.: <i>Z. Phys.</i> , A342 (1992) 342	Pt

Table 4 (continued)

Ho84	B.Hoffmann, et al.: <i>Z. Physik</i> , A315 (1984) 57.....	Polarisation
Hö76	C.Höhle, et al.: <i>Physics Letters</i> , B62 (1976) 390.....	Ba
Hu78	G.Huber, et al.: <i>Phys. Rev.</i> , C18 (1978) 2342.....	Na
Hü78	H.Hühnermann, et al.: <i>Z. Physik</i> , A285 (1978) 229	Xe
Is97	Y.Ishida, et al.: <i>J. Phys.</i> , B30 (1997) 2569.....	Ce
Ji90	Wei Guo Jin, et al.: <i>Journ. Phys. Soc. Jap.</i> , 59 (1990) 3148.....	Er
Ji91	Wei Guo Jin, et al.: <i>Journ. Phys. Soc. Jap.</i> , 60 (1991) 2896.....	Yb
Ji97	W.G.Jin, et al.: <i>Phys. Rev.</i> , C55 (1997) 1545	Hf
Kä89	W.Kälber: <i>Ph.D. Thesis, Univ. Heidelberg, KfK-4513</i> (Februar 1989)	Th
Ke95	M.Keim, et al.: <i>Nucl. Phys.</i> , A586 (1995) 219	Kr
Ki84	W.H.King: <i>Isotope Shifts in Atomic Spectra</i> (Plenum Press, New York, 1984)	Review
Kl79	W.Klempt, et al.: <i>Physics Letters</i> , B82 (1979) 47	Rb
Kl96	A.Klein, et al.: <i>Nucl. Phys.</i> , A607 (1996) 1	Ar
Ko58	H.Kopfermann: <i>Nuclear Moments</i> (Academic Press Inc., New York, 1958)	Basic OIS
Ko91	D.Kowalewska, et al.: <i>Phys. Rev.</i> , A44 (1991) R1442	Po
Kr88	U.Krönert, et al.: <i>Z. Physik</i> , A331 (1988) 521	Au
Kü77	T.Kühl, et al.: <i>Phys. Rev. Letters</i> , 39 (1977) 181	Hg
La92	W.Lauth, et al.: <i>Phys. Rev. Letters</i> , 68 (1992) 1675	Tl
LB97	F.LeBlanc, et al.: <i>Rapport d'activité IPN Orsay, 1996-97</i> , p. 33	Au
LB99	F.LeBlanc, et al.: <i>Phys. Rev.</i> , C60 (1999) 054310.....	Pt
Le88	J.K.P.Lee, et al.: <i>Phys. Rev.</i> , C38 (1988) 2985	Pt
Le99	J.M.G.Levins, et al.: <i>Phys. Rev. Letters</i> , 82 (1999) 2476	Hf
Li91	P.Lievens, et al.: <i>Physics Letters</i> , B256 (1991) 141	Sr
Li92a	P.Lievens, et al.: <i>Europhysics Letters</i> , Submitted, Personal Communication	Kr
Lo85	H.Lochmann, et al.: <i>Z. Physik</i> , A322 (1985) 703	In
Lu94	P.Luc, et al.: <i>Z. Phys.</i> , D31 (1994) 145.....	Ti
Me89	R.Menges: <i>Ph.D. Thesis, Univ. Mainz GSI-89-06</i> (Februar 1989)	Tl, Pb
Me92	R.Menges, et al.: <i>Z. Phys.</i> , A341 (1992) 475	Tl
MH97	Ma Hongliang, et al.: <i>J. Phys.</i> , B30 (1997) 3355.....	Nd
Mu83	A.C.Mueller, et al.: <i>Nuclear Physics</i> , A403 (1983) 234.....	Ba
No77	G.Novicki, et al.: <i>Phys. Rev. Letters</i> , 39 (1977) 332	Ba
No78	G.Novicki, et al.: <i>Phys. Rev.</i> , C18 (1978) 2369.....	Ba
Ok87	H.Okamura, and S.Matsuki: <i>Phys. Rev.</i> , C35 (1987) 1574.....	Er
Pa84	C.W.P.Palmer, et al.: <i>Journ. Phys.</i> , B17 (1984) 2197	Ca
Pa94	G.Passler, et al.: <i>Nucl. Phys.</i> , A580 (1994) 173.....	Au
Re80	H.Rebel, et al.: <i>Nukleonika</i> , 25 (1980) 145	Ba
Ri92	J.Rink: <i>Dissertation, Univ. Heidelberg, KfK 4993</i> (Februar 1992)	Hf
Ri94	E.Riis, et al.: <i>Phys. Rev.</i> , A49 (1994) 207	(From Bu03) Li
Sa90	G.Savard, et al.: <i>Nucl. Phys.</i> , A512 (1990) 241.....	Au
Sa95	C.J.Sansonetti, et al.: <i>Phys. Rev.</i> , A52 (1995) 2682	(From Bu03) Li
Sa00	J.Sauvage, et al.: <i>Hyperfine Interactions</i> , 129 (2000) 303	Rev: Ir, Pt, Au
Sc90	H.A.Schuessler, et al.: <i>Phys. Rev. Letters</i> , 65 (1990) 1332	Kr
Sc96	W.Scherf, et al.: <i>Z. Phys.</i> , D36 (1996) 31	(From Bu03) Li
Si88	S.E.Silverans, et al.: <i>Phys. Rev. Letters</i> , 60 (1988) 2607.....	Sr
Sp89	G.D.Sprouse, et al.: <i>Phys. Rev. Letters</i> , 63 (1989) 1463.....	Yb
St80	A.Steudel, et al.: <i>Z. Physik</i> , A296 (1980) 189.....	Ni
St85	J.Streib, et al.: <i>Z. Physik</i> , A321 (1985) 537	Au
Th81	C.Thibault, et al.: <i>Phys. Rev.</i> , C23 (1981) 2720	Rb
Th81b	C.Thibault, et al.: <i>Nucl. Phys.</i> , A367 (1981) 1	Cs
Th83	R.C.Thompson, et al.: <i>J. Phys.</i> , G9 (1983) 445 [KFK 3455 (Dez. 1982)]	Pb
To82	F.Touchard, et al.: <i>Phys. Rev.</i> , C25 (1982) 2756	Na
To82b	F.Touchard, et al.: <i>Physics Letters</i> , B108 (1982) 169	K
To85	G.Torbohm, et al.: <i>Phys. Rev.</i> , A31 (1985) 2038	Theory: C _i /C ₁ calc.
Ui75	S.Ullrich, and E.W.Otten: <i>Nucl. Phys.</i> , A248 (1975) 173	Cs
Ui85	G.Ulm, et al.: <i>Z. Physik</i> , A321 (1985) 395	In
Ui86	G.Ulm, et al.: <i>Z. Physik</i> , A325 (1986) 247	Hg
Ve92	L.Vermeeren, et al.: <i>Phys. Rev. Letters</i> , 68 (1992) 1679	Ca
Ve99	D.Verney, et al.: <i>Rapport d'activité IPN Orsay, 1998-99</i> , p. 43	Ir
Wa87	K.Wallmeroth, et al.: <i>Phys. Rev. Letters</i> , 58 (1987) 1516.....	Au
Wa89	K.Wallmeroth, et al.: <i>Nucl. Phys.</i> , A493 (1989) 224.....	Au
Wa90	M.Wakasugi, et al.: <i>Journ. Phys. Soc. Jap.</i> , 59 (1990) 2700.....	Nd, Sm, Gd, Dy
Wa03	J.Walls, et al.: <i>Eur. Phys. J.</i> , D22 (2003) 159	(From Bu03) Li
We88	K.Wendt, et al.: <i>Z. Physik</i> , A329 (1988) 407	Ba
Wi58	L.Wilets: <i>Handbook of Physics</i> , 38/1 (1958) 96.....	Basic OIS
Zi80	D.Zimmermann, et al.: <i>Z. Physik</i> , A295 (1980) 307	Lu
Zi94	D.Zimmermann, et al.: <i>Phys. Rev.</i> , A50 (1994) 1112	Hf